

Elliptic Curve Cryptography Based Wireless Authentication Protocol

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Abstract

Recently, Aydos et al. proposed an ECC-based wireless authentication protocol. Because their protocol is based on ECC, the protocol has significant advantage including lower computational burden, lower communication bandwidth and storage requirements. However, Mangipudi et al showed that the protocol is vulnerable to the man-in-the-middle attack from the attacker within the system and proposed a user authentication protocol to prevent the attack. This paper further shows that Aydos et al.'s protocol is vulnerable to man-in-the-middle attack from any attacker not restricted on the inside attacker. Then, a forging certificate attack on Mangipudi et al's protocol is presented. Next, the reasons that Aydos et al's protocol and Mangipudi et al's protocol suffer the attacks are analyzed. Finally, we propose a novel ECC-based wireless authentication protocol and analyze the security of our protocol.

Keywords: Elliptic curve cryptography, key exchange scheme, mutual authentication, security, wireless communication

1 Introduction

With rapid development of communication technology, wireless technology has been widely used in different areas. A problem coming with that is the security of wireless communication system which has drawn more and more attention. Compared with fixed network, wireless communication system is more vulnerable to eavesdropping, intercepting, and unauthorized access. In order to obtain reliable security for wireless communication system, user and system server need to authenticate mutually and establish the session key for subsequent communication. Since the limitation of user's equipment source, e.g., low power capability and small storage, it has caused

more challenges to design an effective Mutual Authentication and Key Establishment Protocol (MAKEP) for wireless communication system. Traditional public key based MAKEP, including Station-to-Station protocol, have provided robust solution to security and authentication in general communication system. However, this kind of protocol has high computational complexity and it will take agency quite a little time to execute the protocol. Meanwhile, the agency's storage room must fulfill a high requirement due to the larger size of key and certificate. Thus the traditional public key based protocol is not suitable for wireless communication system. In private key based MAKEP, two communication parties need to share a long-term key or to have the trusted third party participate when establishing session key. In the first case, to communicate with different parties, each party has to keep a series of different keys. In the latter one, the trusted third party must participate every time when the protocol is executed. Thus these protocols are also not suitable for wireless communication system.

Recently, Aydos et al. proposed an ECC-based wireless authentication protocol [2], and discussed the realization of it in [3]. This protocol has been paid quite a number of attention [4, 6, 7, 11, 12, 13, 14, 15]. This protocol uses elliptic curve digital signature algorithm and Diffie-Hellman key exchange scheme to provide mutual authentication and establish session key. The use of ECC results that this protocol has remarkable advantages to protocols based on RSA or digital signature algorithm (DSA) in terms of performance while providing the same secure level. These advantages include lower computational burden (meaning faster speed), lower bandwidth requirement and lower storage requirement. Unfortunately, there are some serious security deficiencies in this protocol. Sun et al. have proved that this protocol can't provide forward security and known-key security, as well as the mutual identity authentication [8]. Mangipudi et al. have proved

that this protocol is vulnerable to man-in-the-middle attack from attacker within system and proposed a user authentication protocol to prevent man-in-the-middle attack. This paper further shows that Aydos et al.'s protocol is vulnerable to man-in-the-middle attack from any attacker, not restricts to internal attackers. Then, we analyze the protocol proposed by Mangipudi et al and prove that the attacker can pass identity authentication by forging digital certificate. Next, the reasons why both protocols suffer from the attacks are analyzed. Finally, we propose a new ECC-based wireless authentication protocol and analyze the security of our protocol.

2 Theoretic Backgrounds

In this section, we briefly introduce the theoretic background of the protocol proposed by Aydos et al.: Elliptic Curve Diffie-Hellman Key Exchange Scheme (ECDH) and Elliptic Curve Digital Signature Algorithm (ECDSA).

2.1 ECDH

Let $P(x, y)$ be a point with order of n on elliptic curve E which is defined over finite field $GF(p)$, the ECDH can be described as follows:

- 1) S generates a random number $d_S \in [2, n - 1]$, calculates $D_S = d_S P$, and sends D_S to T .
- 2) T generates a random number $d_T \in [2, n - 1]$, calculates $D_T = d_T P$, and sends D_T to S .
- 3) S calculates key $sk_S = d_S D_T$ and T calculates key $sk_T = d_T D_S$.

Since $d_S D_T = d_S d_T P = d_T d_S P = d_T D_S$, thus $sk_S = sk_T$.

2.2 ECDSA

The ECDSA is composed of generate key pair, generate signature, and verify signature.

- Generate key pair:

- 1) Generate a random number $d \in [2, n - 1]$.
- 2) Calculate $Q = dP$.
- 3) Public key is Q , private key is d .

- Generate signature:

In order to sign a message m , entity S operates as follows:

- 1) Generate a random number $k \in [2, n - 1]$.
- 2) Calculate kP .
- 3) Calculate $r = kP.x \bmod n$, where $kP.x$ denotes x coordinate of kP . If $r = 0$, return (1).
- 4) Calculate $s = k^{-1}(h(m) + dr) \bmod n$, where $h(\cdot)$ is a secure hash function. If $s = 0$, return (1). The signature on message m is (r, s) .

- Verify signature:

- 1) Check $r \in [1, n - 1]$, $s \in [1, n - 1]$.
- 2) Calculate $c = s^{-1} \bmod n$.
- 3) Calculate $u_1 = h(m)c \bmod n$ and $u_2 = rc \bmod n$.
- 4) Calculate $R = u_1 P + u_2 Q$.
- 5) Calculate $v = R.x \bmod n$.
- 6) Accept signature if and only if $r = v$.

3 Aydos et al.'s Protocol

Aydos et al. proposed ECC-based wireless authentication protocol in [2]. This protocol can be described as follows.

3.1 Terminal and Server Initialization

When terminal (T) wants to obtain a certificate, T generates a random number $d_T \in [2, n - 1]$, calculates $Q_T = d_T P$, then sends public key Q_T to Certificate Authority (CA) through a secure channel. After receiving the message, CA arranges a unique identity I_T and an expiration time t_T . Then CA generates a random number k_T , calculates $k_T P$, $r_T = k_T P.x \bmod n$, $e_T = h(Q_T.x, I_T, t_T)$ and $s_T = k_T^{-1}(e_T + d_{CA} r_T) \bmod n$, where d_{CA} is the private key of CA, (r_T, s_T) is CA's signature on Q_T . CA sends I_T , t_T , e_T , (r_T, s_T) , and its public key Q_{CA} to T through the secure channel. Repeat the same process, server (S) can obtain its certificate I_S , t_S , e_S , (r_S, s_S) , and CA's public key Q_{CA} .

3.2 Mutual Authentication and Key Agreement

Mutual authentication and key agreement between S and T need to be completed in real time. This process is depicted in Figure 1.

In the protocol, T and S first exchange public key Q_T and Q_S , calculate $Q_k = d_T Q_S$ and $Q_k = d_S Q_T$ respectively. $Q_k.x$ is used as the agreed key. Then, T and S encrypt their own certificate with the agreed key and exchange encrypted certificate respectively. After verifying each other's certificate is valid, T and S calculate session key $sk = Q_k.x + g$.

Compared with RSA-based protocol or DSA-based key agreement protocol, Aydos et al.'s protocol has significant superiorities in terms of speed, storage requirement and bandwidth requirement. However, this protocol is vulnerable to man-in-the-middle attack. This will be described in the next section.

4 Man-in-the-middle Attacks

4.1 Attack from User within System

Mangipudi et al. proposed a man-in-the-middle attack aimed at Aydos et al.'s protocol, this attack requires that

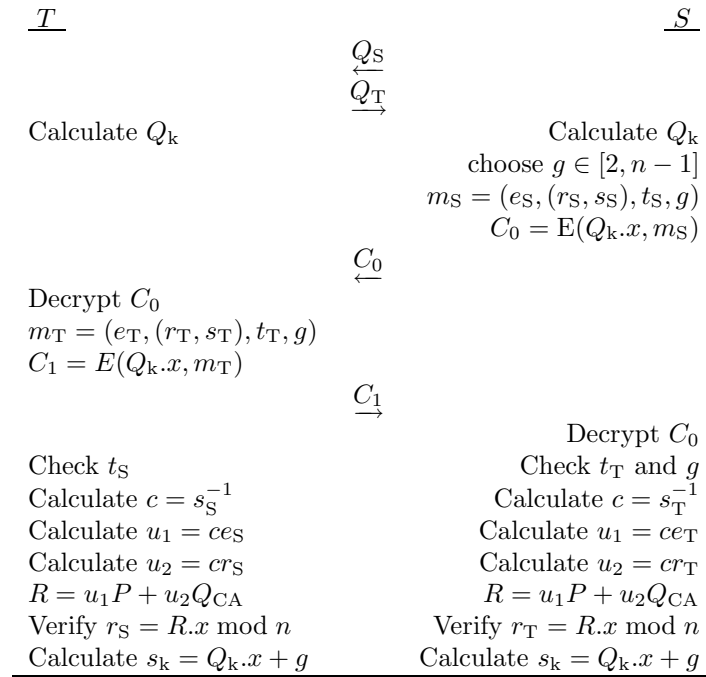


Figure 1: Aydos et al's protocol

attacker M must be a user within system, must have a valid certificate $(e_M, (r_M, s_M), t_M)$. This attack is described as follows (see Figure 2).

- 1) S sends message Q_S to T .
- 2) M intercepts message Q_S , sends message Q_M to T impersonating S , and calculates $Q_{SM} = d_M Q_S = d_M d_S P$.
- 3) T sends message Q_T to S , and calculates $Q_{TM} = d_T Q_M = d_T d_M P$. $Q_{TM} \cdot x$ is used as the agreed key.
- 4) M intercepts message Q_T , sends message Q_M to S impersonating T , and calculates $Q_{TM} = d_M Q_T = d_T d_M P$.
- 5) S calculates $Q_{SM} = d_S Q_M = d_S d_M P$. $Q_{SM} \cdot x$ is used as the agreed key.
- 6) S generates random number g , calculates $C_0 = E(Q_{SM} \cdot x, m_S)$, sends C_0 to T , where $m_S = (e_S, (r_S, s_S), t_S, g)$.
- 7) M intercepts C_0 , decrypts C_0 with $Q_{SM} \cdot x$ to obtain m_S . M checks the validity of t_S , calculates $c = s_S^{-1}$, $u_1 = ce_S$, $u_2 = cr_S$, $R = u_1P + u_2Q_{CA}$, checks whether $r_S = R.x \pmod{n}$ holds. Then, M calculates $C'_0 = E(Q_{TM} \cdot x, m_M)$, sends C'_0 to T , where $m_M = (e_M, (r_M, s_M), t_M, g)$.
- 8) T decrypts C'_0 with $Q_{TM} \cdot x$ to obtain m_M , checks the validity of t_M , calculates $c = s_M^{-1}$, $u_1 = ce_M$, $u_2 = cr_M$, $R = u_1P + u_2Q_{CA}$, checks whether $r_M = R.x \pmod{n}$ holds. Then, T calculates $C_1 = E(Q_{TM} \cdot x, m_T)$, sends C_1 to S , where
- 9) M intercepts C_1 , decrypts C_1 with $Q_{TM} \cdot x$ to obtain m_T . M checks the validity of t_T and g , calculates $c = s_T^{-1}$, $u_1 = ce_T$, $u_2 = cr_T$, $R = u_1P + u_2Q_{CA}$, checks whether $r_T = R.x \pmod{n}$ holds. Then, M calculates $C'_1 = E(Q_{SM} \cdot x, m_M)$, send C'_1 to S , where $m_M = (e_M, (r_M, s_M), t_M, g)$.
- 10) S decrypts C'_1 with $Q_{SM} \cdot x$ to obtain m_M , checks the validity of t_M and g , calculates $c = s_M^{-1}$, $u_1 = ce_M$, $u_2 = cr_M$, $R = u_1P + u_2Q_{CA}$, checks whether $r_M = R.x \pmod{n}$ holds. Then, S calculates $sk_{SM} = Q_{SM} \cdot x + g$. sk_{SM} is used as the session key.

The man-in-the-middle attack from user within system, which is described above, surely threatens protocol to a degree. In order to launch this attack, attacker has to send his own certificate to both communication parties. However, in many cases, malicious attacker doesn't want to leave such "evidence". In fact, the attacker needs not to send his own certificate to communication parties in order to launch the man-in-the-middle attack. We demonstrate this assertion by providing an attack example in next subsection.

4.2 Attack from any Attacker

Before launching attack, the attacker M needs to forge a public key "certificate": generates a random number d_M , calculates $Q_M = d_M P$. When T and S execute proto-

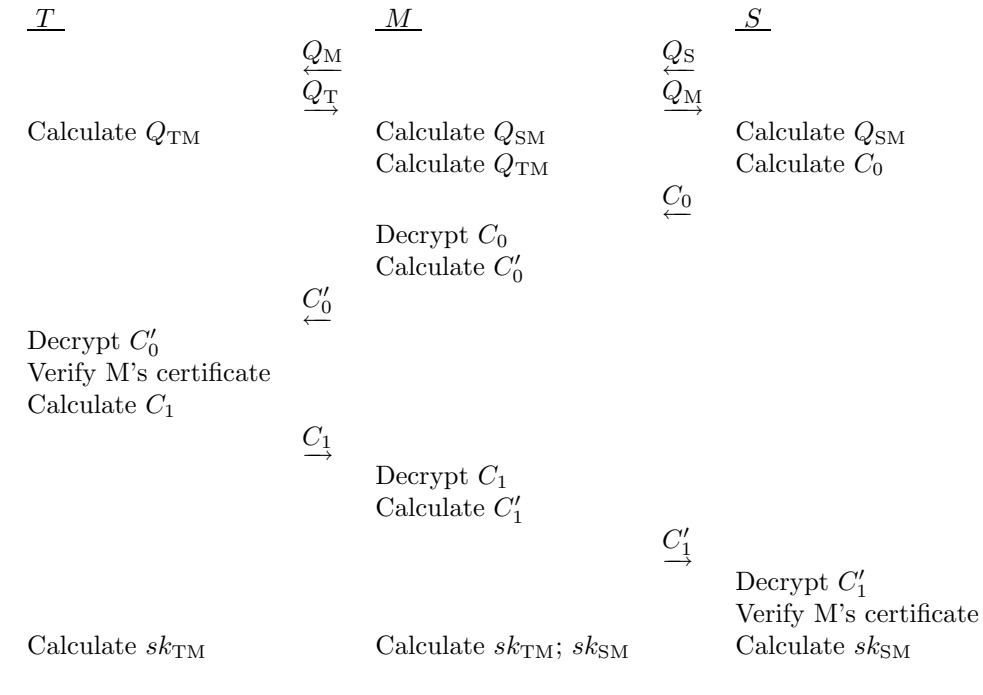


Figure 2: Man-in-the-middle attack from user within system

col, M can launch the man-in-the-middle attack which is described as follows and depicted in Figure 3.

- 1) S sends message Q_S to T .
- 2) M intercepts message Q_S , sends message Q_M to T impersonating S , and calculates $Q_{SM} = d_M Q_S = d_M d_S P$.
- 3) T sends message Q_T to S , and calculates $Q_{TM} = d_T Q_M = d_T d_M P$. $Q_{TM} \cdot x$ is used as the agreed key.
- 4) M intercepts message Q_T , sends message Q_T to S impersonating T , and calculates $Q_{TM} = d_M Q_T = d_T d_M P$.
- 5) S calculates $Q_{SM} = d_S Q_M = d_S d_M P$. $Q_{SM} \cdot x$ is used as the agreed key.
- 6) S generates a random number g , calculates $C_0 = E(Q_{SM} \cdot x, m_S)$, sends C_0 to T , where $m_S = (e_S, (r_S, s_S), t_S, g)$.
- 7) M intercepts C_0 , decrypts C_0 with $Q_{SM} \cdot x$ to obtain m_S . M checks the validity of t_S , calculates $c = s_S^{-1}$, $u_1 = ce_S$, $u_2 = cr_S$, $R = u_1 P + u_2 Q_{CA}$, checks whether $r_S = R \cdot x \pmod{n}$ holds. Then, M calculates $C'_0 = E(Q_{TM} \cdot x, m_S)$, sends C'_0 to T .
- 8) T decrypts C'_0 with $Q_{TM} \cdot x$ to obtain m_S , checks the validity of t_S , calculates $c = s_S^{-1}$, $u_1 = ce_S$, $u_2 = cr_S$, $R = u_1 P + u_2 Q_{CA}$, checks whether $r_S = R \cdot x \pmod{n}$ holds. Then, T calculates $C_1 = E(Q_{TM} \cdot x, m_T)$, sends C_1 to S , where $m_T = (e_T, (r_T, s_T), t_T, g)$. Finally, T calculates $K_{TM} = Q_{TM} \cdot x + g$. K_{TM} is as the session key.

- 9) M intercepts C_1 , decrypts C_1 with $Q_{TM} \cdot x$ to obtain m_T . M checks the validity of t_T and g , calculates $c = s_T^{-1}$, $u_1 = ce_T$, $u_2 = cr_T$, $R = u_1 P + u_2 Q_{CA}$, checks whether $r_T = R \cdot x \pmod{n}$ holds. Then, M calculates $C'_1 = E(Q_{SM} \cdot x, m_T)$, and sends C'_1 to S .
- 10) S decrypts C'_1 with $Q_{SM} \cdot x$ to obtain m_T , checks the validity of t_T and g , calculates $c = s_T^{-1}$, $u_1 = ce_T$, $u_2 = cr_T$, $R = u_1 P + u_2 Q_{CA}$, checks whether $r_T = R \cdot x \pmod{n}$ holds. Then, S calculates $sk_{SM} = Q_{SM} \cdot x + g$. sk_{SM} is as the session key.

The result of the attack described above is that $T(S)$ thinks that the received messages come from $S(T)$ and he shares the same session key K_{TM} (K_{SM}) with $S(T)$. But actually the session key K_{TM} is shared between T and M , and session key K_{SM} is shared between S and M . During the valid period of these two session keys, M can use these two keys to freely eavesdrop the communication between T and S , modify communication messages, or impersonate one party to the other.

5 Mangipudi et al.'s Protocol

Mangipudi et al. proposed a User Authentication Protocol (UAP), which is a variant of Aydos et al.'s protocol. In this protocol, user needs to authenticate himself to server. Similar to Aydos et al.'s protocol, Mangipudi et al.'s protocol is divided into two phases: initialization phase and user authentication phase.

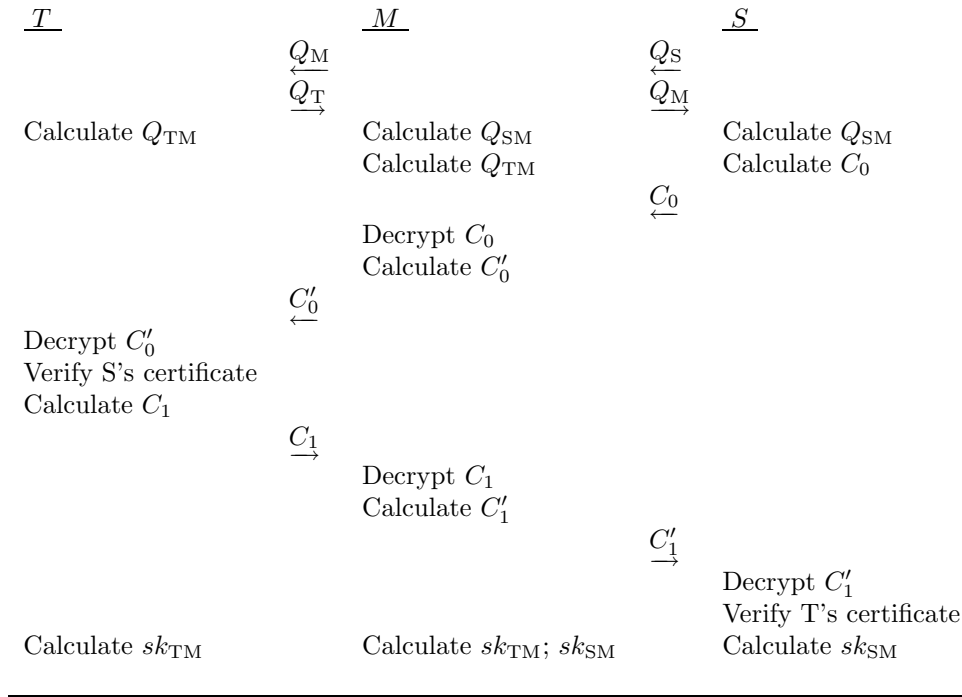


Figure 3: Man-in-the-middle attack from any attacker

5.1 Initialization Phase

Server Initialization Phase: The differences in server initialization phase between Mangipudi et al.' protocol and Aydos et al.'s protocol are: (1) Server needs to calculate the private key d_S 's inversion d_S^{-1} . (2) CA only arranges an identity I_S and an expiration time t_S (not certificate) for server, sends $Q_{C,A}$, I_S , and t_S to server, and stores server's public key Q_S and expiration time t_S .

User Initialization Phase: The differences in user initialization phase between Mangipudi et al.' protocol and Aydos et al.'s protocol is: CA sends server's public key and expiration time, not its own public key, to user.

5.2 User Authentication Phase

The process is as follows and is depicted in Figure 4. User generates a random number $g_T \in [2, n-1]$, calculates $Q_R = g_T Q_S = g_T d_S P$, sends Q_R to server, and calculates $Q_{TS} = g_T P$. $g_{TS} = Q_{TS}.x$ is used as the agreed key. After receiving message, server calculates $d_S^{-1} Q_R$ to obtain the agreed key g_{ST} . Then, server encrypts the message m_S with agreed key to obtain $C_0 = E(g_{ST}; m_S)$, sends C_0 to user, where $m_S = (g_{TS}, g_S, t_S)$, g_S is a random number generated by server, $g_S \in [2, n-1]$. User decrypts C_0 with agreed key g_{TS} to obtain m_S , checks the validity of g_{TS} and t_S . Then, user encrypts message m_T with g_{TS} to obtain $C_1 = E(g_{TS}; m_T)$, where $m_T = (e_T, (r_T, s_T), t_T, g_S)$, sends C_1 to server, and calculates session key $sk_{TS} = h(g_{TS}, g_S)$. Server decrypts C_1 , checks the validity of g_S and t_T , verifies user's certificate. Then, server calculates session key $sk_{ST} = h(g_{ST}, g_S)$.

6 Attack to Mangipudi et al.'s Protocol

Mangipudi et al.'s protocol is robust to man-in-the-middle attack. However, this protocol is vulnerable to the forging certificate attack launched by attacker after he has forged the certificate. To make it easy to be understood, we present a simple way of forging certificate here. Let $e_M = 0$, $r_M = Q_{C,A}.x$, $s_M = r_M$, M uses $(e_M, (r_M, s_M))$ as the forging certificate, and forges an expiration time t_M for this certificate. Then, M can use forging certificate to impersonate a legal user to server. This attack is described as follows and is depicted in Figure 5.

- 1) M generates a random number $g_M \in [2, n-1]$, calculates $Q_R = g_M Q_S$, sends Q_R to server, and calculates $Q_{MS} = g_M P$. $g_{MS} = Q_{MS}.x$ is as the agreed key.
- 2) Server calculates $Q_{SM} = d_S^{-1} Q_R = g_M P$. $Q_{SM}.x$ is as the agreed key. Then, server calculates $C_0 = E(g_{SM}, m_S)$, sends C_0 to M , where $m_S = (g_{SM}, g_S, t_S)$, g_S is random number generated by server.
- 3) M decrypts C_0 with the agreed key Q_{SM} to obtain m_S , checks the validity of g_{SM} and t_S . Then, M encrypts message $m_M = (e_M, (r_M, s_M), t_M, g_S)$ with g_{SM} to obtain $C_1 = E(g_{SM}; m_M)$, sends C_1 to server, and calculates session key $sk_{MS} = h(g_{MS}, g_S)$.
- 4) Server decrypts C_1 , check the validity of g_S and t_M , calculates $c = s_M^{-1}$, $u_1 = ce_M = 0$, $u_2 = cr_M = 1$, $R = u_1 P + u_2 Q_{CA} = Q_{CA}$, $v = R.x = Q_{CA}.x$, verify

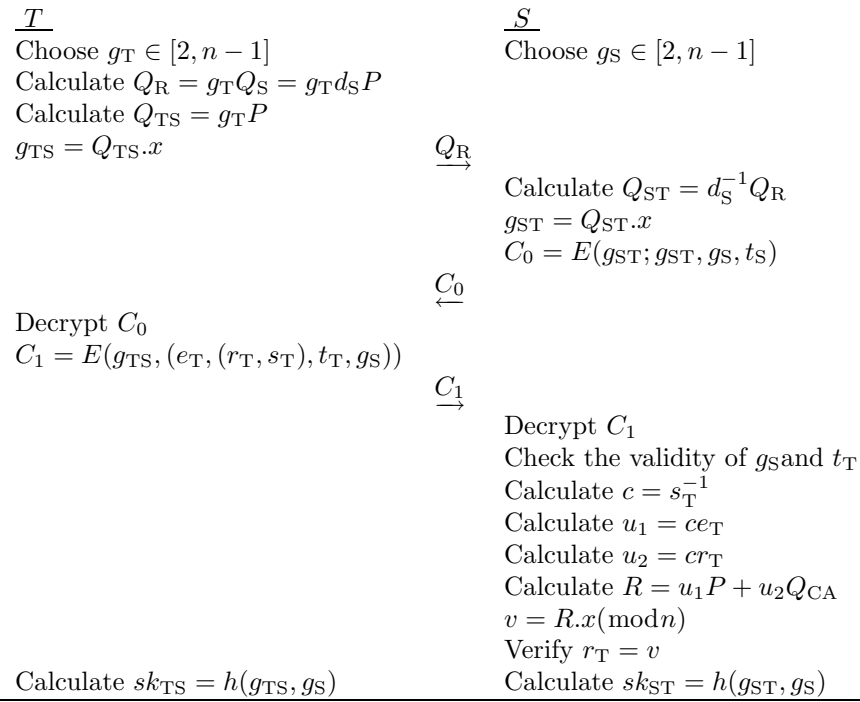


Figure 4: Mangipudi et al.'s user authentication protocol

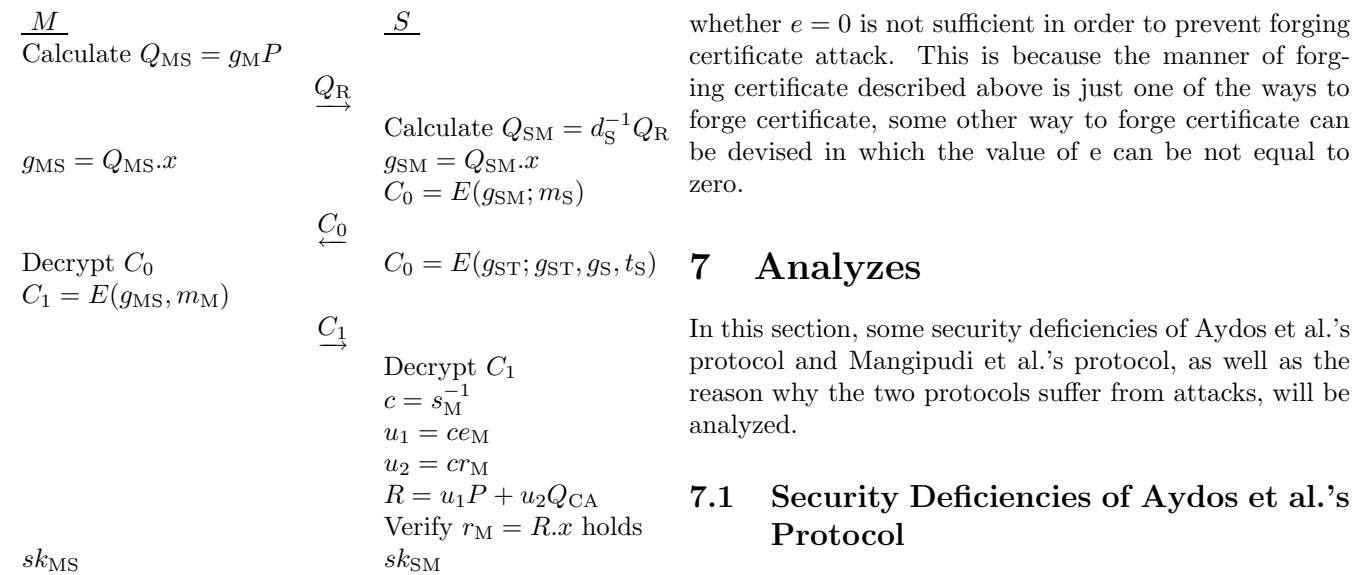


Figure 5: Mutual authentications and key agreement

whether the equation $r_M = v$ holds. According to the manner in which M forges certificate, $r_M = v$ holds. Thus, M has passed the identity authentication to server. Finally, server calculates session key $sk_{SM} = h(g_{SM}, g_S)$.

Through the way of forging certificate described above, M can successfully pass server's authentication. This is surely a very serious threat to Mangipudi's protocol. What worth being paid attention is that only checking

The security deficiencies of Aydos et al.'s protocol can be explained from two aspects: design principle and design details of the protocol.

- Deficiency of design principle:
 The design principle of Aydos et al.'s protocol is that both communication parties exchange public key to establish the agreed key, then exchange certificate to verify each one's identity, and finally calculate session key using both the agreed key and random number. In which, certificates are exchanged in their encrypted form. This not only provides the secrecy of the certificate, but also provides (agreed) key confirmation to both parties. With the assumption that the agreed key won't be disclosed, this de-

sign principle can achieve entity authentication [8]. This is because: (1) Certificate assures authenticity and coupling of entity identity and its public key. (2) Key confirmation makes both two parties believe that each other has the private key corresponding to public key included in certificate. (3) Using nonce random number ensures the freshness of message. Thus, with the assumption described above, this design principle can achieve entity authentication. However, this assumption isn't tenable. Since public key information is changeless, so the agreed key computed from public keys of two parties is constant. Therefore the agreed key may be disclosed (Taking the principle of being prudent into consideration, many protocol designers assume that long term public key (Q_S and Q_T) is much possible to be disclosed). In the case of that agreed key is possible to be disclosed, the protocol can't achieve entity authentication. For example, the attacker can use Alice's certificate eavesdropped to impersonate Alice to Bob under the assumption that the agreed key between Alice and Bob was disclosed.

- Deficiencies in design details:

Even under the assumption that agreed key won't be disclosed, some deficiencies in design details of this protocol can still induce the protocol to be unable to achieve entity authentication.

- 1) This protocol can not provide entity authentication of server to terminal. The nonce random number generated by server is included in message C_1 which is returned to server by terminal, thus server knows the current message is fresh, this makes it possible for protocol to provide entity authentication of terminal to server. However, the same mechanism is not introduced into the authentication of server to terminal. Thus, the terminal can only obtain the message origination authentication at most, and it can't obtain the entity authentication of server. Since terminal can't make sure whether the message is fresh, the attacker may send old message again to deceive.
- 2) There are some problems in the entity authentication because it is impossible for verifier to obtain any identity information of the other party. In protocol, to satisfy the anonymity requirement, both parties only exchange public key and certificate, but don't exchange identity information (They can't learn identity information from certificate). In this case, both communication parties can't know any identity information of the other party. This induces that the protocol is vulnerable to man-in-the-middle attack from user within system, which is proposed by Mangipudi et al.
- 3) The verification for public key certificate is un-

reasonable, and there is no way to verify the association between public key certificate and public key. Usually, a public certificate contains messages such as entity identity, public key, and expiration time, and so on. It also contains CA's signature on these messages. Entity identity and its public key are associated closely by signatures. And the signature illuminates that the public key in certificate is issued to the entity whose identity is included in certificate. In the protocol, CA issues certificate $(e, (r, s), t)$ to entity, where $e = h(Q, I, t)$, (r, s) is CA's signature on e . When verify certificate, since both communication parties haven't exchanged identity information, both of them can't verify the association between e and Q (can't verify whether e is surely obtained by calculating the hash value of the other party's identity, public key and expiration time), and can't make sure whether the public key certificate is issued for the other party's either. This induces that this protocol is vulnerable to the man-in-the-middle attack presented in this paper.

Due to the deficiencies in design principle and design details, besides can't provide entity authentication, Aydos et al.'s protocol can't satisfy some basic security aims either, including explicit key authentication, forward security, known-key security, key control, and so on.

7.2 Security Deficiencies of Mangipudi et al.'s Protocol

Mangipudi et al.'s protocol is the variant of Aydos et al.'s protocol, and it can resist man-in-the-middle attack. However, there are still some vital security deficiencies in this protocol, including deficiencies inherited from Aydos et al.'s protocol and deficiencies in the protocol itself.

Firstly, this protocol doesn't provide user's entity authentication to server. The reasons are similar to (2) and (3) in Section 7.1.2. This allows attacker to forge a certificate and use it to pass server's identity authentication.

Secondly, this protocol doesn't provide forward security because disclosing server's secret key d_S or d_S^{-1} will lead to all previous secret information being disclosed.

Thirdly, this protocol doesn't provide explicit (session) key authentication. This makes both communication parties can't know whether the other party exactly calculates the session key.

Fourthly, it is difficult to implement the renewal for security of wireless communication system based on this protocol. Once server's secret key is disclosed, all previous communication messages between users and server, including the user's certificate, will be disclosed. In this case, just updating server's secret key isn't sufficient because the attacker can use the disclosed certificate to impersonate authorized user to server. Thus, the system has to be updated entirely. Compared with this protocol,

many protocols such as Station-to-Station protocol only need to update the disclosed long-term secret key. At this point, there is quite a deficiency in this protocol.

8 Our Protocol

8.1 The Description of Our Protocol

In this section, we will propose a novel ECC-based key establishment protocol. Our protocol takes station-to-station protocol as the basic framework. In order to prevent Lowe attack [9], the communication parties' identity information is added into the signature message. Meanwhile, to make it more efficient to execute, this protocol uses one of the most efficient signature schemes, Schnorr signature scheme [10], as digital signature algorithm

Assume that terminal T and server S respectively get certificate $C(T)$ and $C(S)$ from certificate authority. In our protocol, terminal and server execute steps as follows, and it is depicted in Figure 6.

- 1) T executes precomputation: generates random number $y \in [1, n - 1]$, calculates $Y = yP$; generates random number b , calculates $(b_1, b_2) = bP$ and $b' = b_1 \pmod{n}$.
- 2) T sends Y to S .
- 3) S generates a random number $x \in [1, n - 1]$, calculates $X = xP$.
- 4) S calculates $K = yX = yxP$, K is as session key shared by T and S (In practice, session key is generated by a key derivation function). S calculates the signature on (X, Y, I_S) : (5) and (6).
- 5) S generates random number a , calculates $(a_1, a_2) = aP$ and $a' = a_1 \pmod{n}$. Then S calculates $g = h(a', X, Y, I_S)$. If $g = 0$, executes this step again, otherwise, goes on executing the following protocol.
- 6) S calculates $v = (a - d_S g) \pmod{n}$. (a', v) is as S 's signature on message (X, Y, I_S) .
- 7) S uses symmetric encryption algorithm, such as AES, to encrypt $C(S)$ and (a', v) with K . The encryption result is $E_K(C(S), (a', v))$.
- 8) S sends message X and $E_K(C(S), (a', v))$ to T .
- 9) T calculates session key $K = yX = xyP$, decrypts $E_K(C(S), (a', v))$ with K to get $C(S)$ and (a', v) . T verifies certificate $C(S)$. If the verification result is wrong, the protocol will be terminated. Otherwise, the protocol will be continued. T verifies S 's signature: (10)-(12).
- 10) T checks $a', v \in [1, n - 1]$.
- 11) T calculates $g = h(a', X, Y, I_S)$, $t_1 = v \pmod{n}$, $t_2 = g \pmod{n}$ and $(x_1, x_2) = t_1P + t_2Q_S$.
- 12) T checks whether $a' = x_1 \pmod{n}$ holds. If it doesn't hold, the protocol will be terminated. Otherwise, the protocol will be continued. T calculates signature on (Y, X, I_T, I_S) : (13)-(14).
- 13) T calculates $g = h(b', Y, X, I_T, I_S)$.
- 14) T calculates $u = (b - d_T g) \pmod{n}$. (b', u) is used as T 's signature on (Y, X, I_T, I_S) .
- 15) T uses symmetry encryption algorithm to encrypt $C(T)$ and (b', u) with K , sends $E_K(C(T), (b', u))$ to S .
- 16) S decrypts $E_K(C(T), (b', u))$ with K and gets $C(T)$ and (b', u) .
- 17) S checks the validity of $C(T)$. If $C(T)$ is a valid certificate, the protocol will be continued. Otherwise, the protocol will be terminated. S verifies T 's signature: (18)-(20).
- 18) S checks $b', u \in [1, n - 1]$.
- 19) S calculates $f = h(b', Y, X, I_T, I_S)$, $t_1 = u \pmod{n}$, $t_2 = f \pmod{n}$, and $(x_1, x_2) = t_1P + t_2Q_S$.
- 20) S checks whether $b' = x_1 \pmod{n}$ holds.

8.2 Security Analysis of our Protocol

- Entity authentication and explicit key authentication:

In our protocol, T first sends message Y to S . Once receiving the message, S calculates session key K . Under the assumption that it is difficult to calculate elliptic curve discrete logarithm problem, S believes that only the party, who created the message, can calculate the shared session key exactly. After that, S calculates the signature (a', v) on message (X, Y, I_S) , encrypts certificate $C(S)$ and signature (a', v) with session key K , and sends X and $E_K(C(S), (a', v))$ to T . T calculates session key K , and decrypts the received message with K . After verifying certificate and signature, T makes sure that S is legal intended server, no other than S can calculate the session key shared with it, and S has calculated session key exactly. Therefore, our protocol has provided S 's entity authentication and explicit key authentication to T . Then, T calculates the signature (b', u) on (Y, X, I_T, I_S) , encrypts certificate $C(T)$ and signature (b', u) with session key K , and sends $E_K(C(T), (b', u))$ to S . S decrypts the received message with session key K , and gets $C(T)$ and (b', u) . After verifying certificate and signature, S is sure that T is a legal terminal, only T can calculate the session key shared with it, and T has calculated session key exactly. Therefore, our protocol has provided T 's entity authentication and explicit key authentication to S . In a word, our protocol has provided entity authentication and definite key authentication to both of communication parties.

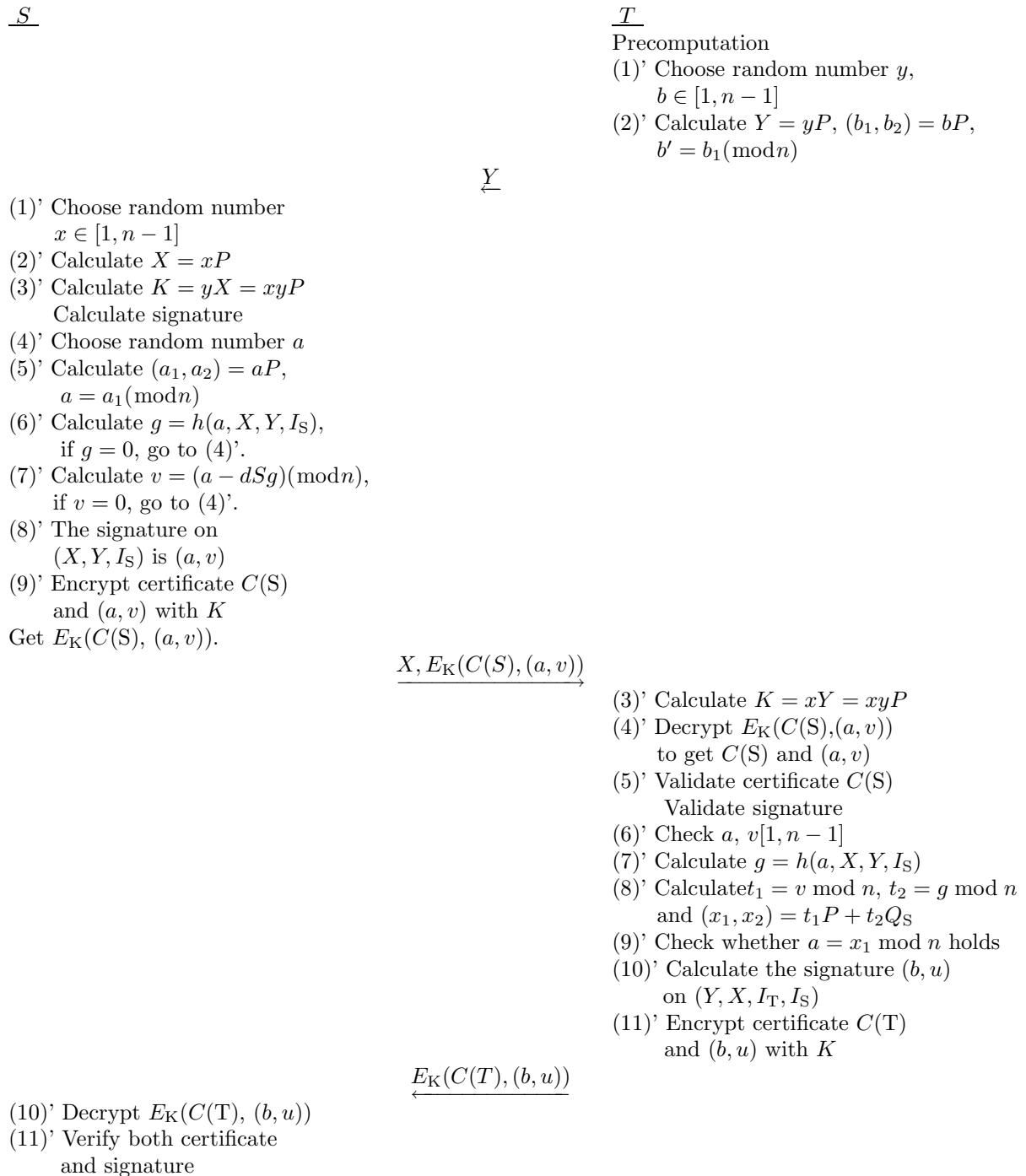


Figure 6: Our protocol

- Known key security:

We show that our protocol possesses the known key security property from two aspects.

- 1) In our protocol, session key is calculated from the random numbers generated by the two communication parties every time. If random number generator or algorithm is good enough, then the probability that the same session keys are generated in two runs of our protocol is neglectable. Therefore, from this point, it is impossible to learn other keys when knowing several session keys.
- 2) Our protocol's security depends on the difficulty of calculating elliptic curve discrete logarithm problem. Knowing several session keys is not helpful to decrease the difficulty of calculating elliptic curve discrete logarithm problem. Therefore, even though attacker has known several session keys, he can't know other session keys.

- Forward secret:

In our protocol, session key is calculated from the random numbers generated by the two communication parties every time. Therefore, the disclosure of secret information won't lead to the disclosure of previous session keys.

- Key compromise impersonation:

In our protocol, the secret information of both communication parties is bounded with certificate. Therefore, using its secret information or other secret information it gets through certain manner, the attacker can't impersonate other party besides the owners of secret information. That is to say, our protocol can prevent key compromise impersonation.

- Unknown key share:

In our protocol, both parties' public key and secret key are unique. What's more, messages in this protocol contain the identities of both communication parties, and the protocol has provided explicit key authentication. Therefore, our protocol is robust to the unknown key share attack based on public key substitution and based on duplicate-signature key selection [17].

- Key control:

In our protocol, session key is calculated from the random numbers generated by both parties, and both random numbers have coequal effect on generation of session key. Therefore, any party can't force the session key to be a value chosen beforehand.

- Terminal's anonymity:

In our protocol, terminal T's public key certificate is sent to server S in the encryption form. This has prevented attacker from eavesdropping terminal identity

information. Therefore, our protocol has provided terminal's anonymity.

All the characters described above have ensured that our protocol satisfies the basic security requirement and is robust to the existing attacks.

9 Conclusions

In this paper, we have proved Aydos et al.'s protocol is vulnerable to man-in-the-middle attacks from any attacker not restricted on attacker within system. Next, we proposed a forging certificate attack to Mangipudi et al.'s protocol. Then, we analyzed the reasons why Aydos et al.'s protocol and Mangipudi et al.'s protocol suffer from attacks and pointed out some other deficiencies in these two protocols. Finally, we propose a new ECC-based wireless authentication protocol and analyze the security of our protocol. The analysis result shows that our proposal satisfies the basic security requirement and is robust to the existing attacks.

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