# Constructing Provably Secure ID-based Beta Cryptographic Scheme in Random Oracle

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## Abstract

In this study, we propose a new ID-based beta cryptosystem scheme secure under selective identity adaptive chosen ciphertext security (IND-sID-CCA) under assumption in the random oracle model. We demonstrate that our scheme outperforms the other existing schemes in terms of security, computational cost and the length of public key.

Keywords: Discrete Logarithm Problem; Generalized Discrete Logarithm Problem; ID-based Cryptosystem; Integer Factorization Problem and Beta Cryptosystem; Public key Cryptosystem

# 1 Introduction

Shamir [24] introduced the idea of ID-based cryptography to simplify the key management problem in 1984. Two efficient ID-based cryptosystem schemes were proposed by Cocks [7] and Boneh and Franklin [6] in 2001. In their seminal paper [5], Boneh and Franklin used a category of bilinear maps as the basis of their construction. This leads a number of ID-based cryptosystem schemes [2, 3, 26], among others based on bilinear maps. Few ID-based cryptosystem schemes [1, 10, 12] have been proposed after 2003. But in these schemes, the public key of each user is not only an identity, but also some random number selected either by the user or by the trusted authority. But which makes the ID-based cryptosystem an active research field in recent years.

The first efficient ID-based cryptosystem scheme was proposed by Boneh and Franklin [5, 6]. The novel approach they use is based on a class of bilinear maps. Following their work, a number of ID-based cryptosystem scheme using bilinear maps were proposed. For example,Waters [12] presented an efficient and secure ID-based cryptosystem scheme without random oracles; Boneh and Boyen [2] designed a secure ID-based cryptosystem scheme without random oracles; Boneh and Boyen [3] gave another efficient ID-based encryption scheme without random oracles, which is secure in the selective identity model.

Meshram *et al.* [17, 20, 22] presented some new efficient ID-based cryptographic schemes and ID-based mechanisms based on discrete logarithm problem, generalized discrete logarithm problem and integer factorization problem. The security of this schemes are solving the hardness of discrete logarithm problem, generalized discrete logarithm problem and integer factorization problem simultaneously. Meshram and Meshram [18, 19] investigate the new variant of ID-based beta cryptographic scheme and transformation process such as public key cryptographic scheme transfer to ID-based cryptographic scheme without developing new ID-based scheme.

Meshram [14, 15, 16] presented new provably secure ID-based cryptographic scheme, new variant of ID-based beta cryptographic scheme, and efficient scheme based on integer factorization problem and discrete logarithm problem. It is as low as ElGamal scheme. Meshram and Obaidat [21] also showed new variant of ID-based cryptographic scheme such as quadratic-exponentiation randomized cryptographic scheme. Recently, Meshram *et al.* [23] projected new ID-based cryptographic scheme based on partial discrete logarithm problem. Liu and Ye [11] presented new variations as homomorphic universal re-encryptor for ID-based cryptography. In similar manner Wang *et al.* [25] presented efficient ID-based proxy multi signature using cubic residues.

As outlined above, unfortunately we found that new cryptographic model always face security challenges and confidentiality concerns. Therefore, our main contribution of this paper is to fill this gap by proposing a provably secure ID-based beta cryptographic scheme. Specifically, we will show that the security of the proposed scheme is closely, if not tightly, related to difficulty of solving generalized discrete logarithm problem and integer factorization problem. We provided an formal security proof for selective identity adaptive chosen ciphertext security (INDsID-CCA) in the random oracle, which means that the new scheme offers better security guarantees than existing other ID-based cryptographic schemes. The proposed scheme does not use pairings (bilinear maps), resulting in high efficiency and ease of implementation, neither does it rely on the relatively new and untested hardness assumptions related to pairing-based cryptography. This makes it attractive for application in resource-constrained environments where saving in computation, communication and implementation code area is a premium.

The rest of this paper is organized as follows: The Beta cryptosystem and supporting example for it are demonstrated in Section 2 and 3 respectively. Proposed an ID-based beta cryptographic scheme with chosen ciphertext security is demonstrate in Section 4. The security examination of proposed ID-based cryptographic scheme is presented in Section 5. Discuss comparison with previous ID-based cryptographic schemes in Section 6. Finally, Section 7 concludes the paper.

# 2 The Beta Cryptosystem

The algorithm consists of three sub-algorithm, Key generation, Encryption and Decryption.

### 2.1 Key Generation

The key generation algorithm runs as follows (user 1 should do the following).

- 1) Select arbitrary primes q and p each roughly of the same size.
- 2) Calculates  $N = q \star p$  and Euler-phi function  $\varphi(N) = (q-1)(p-1)$ .
- 3) Choose an arbitrary integer  $e, 1 \leq e \leq \varphi(N)$  such that gcd  $(e, \varphi(N)) = 1$ .
- 4) Choose an arbitrary integer b such that  $2 \leq b \leq \varphi(N) 1$ .
- 5) Choose an element  $\beta$  of the multiplicative group  $\mathbb{Z}_N^*$ and calculate  $y_1 = \beta^b mod(N)$ .
- 6) By using the extended Euclidean algorithm to calculate the unique integer  $d, 1 \leq d \leq \varphi(N)$  such that  $ed \equiv 1(mod\varphi(N)).$

The public key is formed by  $(N, e, \beta^b)$  and the corresponding private key is given by  $(d, b, \beta)$ .

### 2.2 Encryption

An user 2 to encrypt a message m to user 1 should do the following:

- 1) The message is represented as an integer in the interval [1, N-1].
- 2) The cipher text is given by  $C = (m\beta^b)^e mod(N)$ .

### 2.3 Decryption

To recover the plaintext m from the cipher text C, user 1 should do the following:

- 1) Calculate  $y_2 = \beta^{\varphi(N)-b} mod(N) = \beta^{-b} mod(N)$ .
- 2) Then calculate  $y_3 = (y_2)^e mod(N)$ .
- 3) Recover the plaintext m by computing  $((y_2)^e \star C)^d (modN)$ .

# 3 Example

To make our construction easy to comprehend, we illustrate an example to show the basic principle of our proposed scheme.

Let the two primes be q = 29 and p = 43 and set N = 1247 and  $\varphi(N) = 1176$ .

### 3.1 Key Generation

The key generation algorithm runs as follows.

- 1) Select an arbitrary integer e = 11 and gcd (11, 1176) = 1.
- 2) Select an arbitrary integer b = 19.
- 3) Choose an element  $\beta = 10$  of the multiplicative group  $\mathbb{Z}_N^*$  and calculate  $y_1 = \beta^b mod(N) = (10)^{19} mod \ 1247 = 427.$
- 4) By using the extended Euclidean algorithm to compute the unique integer  $d = 107, 1 \le d \le \varphi(N)$  such that  $11d \equiv 1 \pmod{1176}$ .

The public key is formed by  $(N, e, \beta^b)$  and the corresponding private key is given by  $(d, b, \beta)$ .

### 3.2 Encryption

An user 2 to encrypt a message m to user 1 should do the following:

- 1) The message m = 1122 is represented as an integer in the interval [1, N - 1].
- 2) The cipher text is given by  $C = (m\beta^b)^e mod(N) = (479094)^{11} mod \ 1247 = 791.$

#### Decryption 3.3

To recover the plaintext m from the cipher text C, user Let C be the valid ciphertext encrypted by using the pub-1 should do the following:

- 1) Calculate  $y_2 = \beta^{\varphi(N)-b} mod(N) = \beta^{-b} mod(N) =$ 917.
- 2) Then calculate  $y_3 = (y_2)^e mod(N) = 483$ .
- 3) Recover the plaintext m by computing  $((y_2)^e \star$  $C)^d(modN) = 1122.$

### 4 An ID-based Beta Cryptosystem Scheme with Chosen Ciphertext Security

The major contribution of our proposed ID-based beta cryptosystem is the key generation phase. Upon the successful creation of a private key, the scheme concept can be easily implemented in encryption and decryption posses.

#### **4.1** Setup

By taking in security parameter t this algorithm will be carried out by PKG as follows:

- 1) Let N = q \* p be a large prime number, such that  $\varphi(N) = (q-1)(p-1)$  and  $\beta$  be an element of order N in  $Z_N^{\star}$ , x, y be PKG's secret and public keys respectively, where  $y = \beta^x \mod N$ .
- 2) Select two random integers e and d as  $1 \leq e, d \leq$  $\varphi(N)$ , such that  $gcd(e,\varphi(N)) = 1$  and  $ed \equiv$  $1(mod\varphi(N)).$
- 3) The PKG chosen randomly secret information as  $k_i$ for  $(1 \leq i \leq t)$ , where  $\Sigma_{i=1}^{t} k_i < \varphi(N)$  and public *t*).
- 4) Compute the hash function  $H: \{0, 1\}^t \to Z_N^*$ .

#### 4.2Exact

For a given user identity  $ID \in \{0,1\}^*$ , we compute the private key of the user is  $\beta^{\theta_A} = v K_A^{K_A} mod N$ , where  $\theta_A = \sum_{i=1}^t k_i v_{Ai} mod \varphi(N)$ ,  $K_A = \prod_{i=1}^t K_i^{v_{Ai}} mod N$  and  $v_{Ai}$  is the  $i^{th}$  bit of  $H(ID_A)$  for  $(1 \le i \le t)$ .

#### Encryption 4.3

To encrypt a message  $M \in \{0, 1\}^*$  for ID as follows:

- 1) Set the public key  $V_A = \beta^{\theta_A} = v K_A^{K_A} mod N$ , where  $K_A = \prod_{i=1}^t K_i^{v_{Ai}} mod N$ .
- 2) Chosen a random integer e such that  $gcd(e, \varphi(N)) =$ 1.
- 3) Compute the ciphertext be Cto =  $(M\beta^{\theta_A})^e (mod \ N).$

#### 4.4 Decryption

lic key  $V_A$ . The user can decrypt ciphertext using the private key  $\theta_A$ .

- 1) Calculate  $y_2 = \beta^{-\theta_A} \pmod{N}$ .
- 2) Compute  $y_2^e = (\beta^{-\theta_A})^e \pmod{N}$ .
- 3) Out put M as the decryption of C as

$$[(y_2)^e * C]^d (mod \ N) = [\beta^{-\theta_A e} M^e \beta^{\theta_A e}]^d (mod \ N)$$
$$= M^{ed} (mod \ N) = M (mod \ N).$$

#### $\mathbf{5}$ Security Examination

In this section, we examine the security of ID-based beta cryptosystem scheme. The following theorem shows that ID-based beta cryptosystem scheme is IND-sID-CCA secure, if beta cryptosystem is IND-CCA secure [8] in random oracle model [9].

**Definition 1.** An ID-based cryptosystem scheme, E is said to be selective identity, adaptively chosen ciphertext secure (IND-sID-CCA), if no probabilistic polynomial time (PPT) adversary A has a non-negligible advantage in the following game in [4].

**Theorem 1.** The identity hash function H be a random oracle. Then ID-based beta cryptosystem scheme is INDsID-CCA secure, if beta cryptosystem [Section 2] is IND-CCA secure. Concretely, suppose there is an IND-sID-CCA rival  $R_1$  that has advantage  $\epsilon(k)$  against ID-based beta cryptosystem. Then there exists an IND-CCA rival  $R_2$  with advantage at least  $\epsilon(k)$  against beta cryptosystem. Its running time is rival  $O(time(R_1))$ .

*Proof.* The main idea of this proof is to construct an IND-CCA rival  $R_2$  to gain the advantage against beta cryptosystem in the following IND-CCA game.

At the starting of the game, the IND-CCA challenger generates the public key  $K_{pub} = \langle N, \beta, v \rangle$  and a private key x that satisfies  $v = \beta^x \mod N$ . The challenger gives  $K_{pub}$  to rival  $R_2$ , then rival  $R_2$  mounts an IND-CCA attack using the help of algorithm rival  $R_1$  as follows:

- **Initialization.** The rival outputs an identity  $ID_{ch}$  which it wishes to be challenged.
- **Setup.** The challenger runs the *setup algorithm*. It gives the rival the resulting system parameters. It keeps the masterkey to itself.
- **H-queries.** To respond to H-query,  $R_2$  maintains a list of tuples  $\langle ID_{Ai}, V_{Ai}, \theta_{Ai} \rangle$  which we refer to as  $H^{list}$ . The list is initially empty. When  $R_1$  queries H at a point  $ID_{Ai}$ ,  $R_2$  responds as follows:
  - 1) If the query on  $ID_{Ai}$  already appears on the  $H^{list}$  in a tuple of the form  $\langle ID_{Ai}, V_{Ai}, \theta_{Ai} \rangle$  then  $R_2$  responds with  $H(ID_{Ai}) = v_{Ai}$  as a answer.

- 2) If the query is new to the H oracle,  $R_2$  will pick a random  $\theta_{Ai} \in Z_N^*$  and computes  $V_{Ai} =$  $\beta^{\theta_{A_i}} mod N$ , else  $R_2$  sets  $\theta_{A_i} = *$  and  $V_{A_i} = v$ . as a answer. Here \* denotes a special symbol.
- 3)  $R_2$  adds the tuple  $\langle ID_{Ai}, V_{Ai}, \theta_{Ai} \rangle$  to  $H^{list}$  and gives back  $V_{Ai}$  to  $R_1$ .
- **Phase 1-Extraction queries.** When  $R_1$  asks for the private key associated to  $ID_{Ai}$ ,  $R_2$  runs the above algorithm and gets  $H(ID_{Ai}) = v_{Ai}$ , where  $\langle ID_{Ai}, V_{Ai}, \theta_{Ai} \rangle$  is the corresponding entry in  $H^{list}$ . As  $V_{Ai} = \beta^{\theta_{Ai}} mod N$ ,  $R_2$  can retrieve the legitimate private key  $\theta_{Ai}$  for  $ID_{Ai}$ . The extraction query on  $ID_{ch}$  will be denied.
- **Phase 1-Decryption queries.** Let  $\langle ID_{Ai}, C_i \rangle$  be a decryption query issued by adversary  $R_1$ , where C is ciphertext of beta cryptosystem.  $R_2$  responds to the query as follows:
  - 1) If  $\langle ID_{Ai} \neq ID_{ch} \rangle$ , then  $R_2$  runs *H*-query algorithm such that of the form  $\langle ID_{Ai}, V_{Ai}, \theta_{Ai} \rangle$  be the corresponding tuple on  $H^{list}$ . Next it uses the private key  $\theta_{Ai}$  to respond to the decryption query.
  - 2) If  $\langle ID_{Ai} = ID_{ch} \rangle$ , then  $R_2$  forwards the decryption query with  $\langle C_i \rangle$  and then relays the challenger's response back to  $R_1$ .
- **Challenge.** Once  $R_1$  decides that Phase 1 is over it outputs two messages  $M_0$  and  $M_1$  which it wishes to be challenged on. Algorithm  $R_2$  responds as follows:
  - 1)  $R_2$  gives the challenger  $M_0$  and  $M_1$  as the messages that it wishes to be challenged on. The challenger responds with the beta cryptosystem's ciphertext C such that C is the encryption of  $M_c$  for a random coin  $c \in \{0, 1\}$ .
  - 2) Next,  $R_2$  runs the algorithm for responding Hqueries to obtain  $v \in Z_N^*$  such that  $H(ID_{ch}) =$ v and forwards C to  $R_1$ .
- **Phase 2-Extraction queries.**  $R_2$  responds the same as in Phase 1, except for the extraction query on  $ID_{ch}$ , which will be rejected.
- **Phase 2-Decryption queries.**  $R_2$  responds the same as in Phase 1 except the decryption query  $\langle ID_{ch}, C \rangle$ will be denied.
- **Guess.** Rival  $R_1$  finally outputs a guess c' for c. Rival  $R_2$  outputs c' as its guess for c.

The responses to H-queries are as in the factual attack since each response is uniformly and independent distributed in  $Z_N^*$ . All responses to private key extraction queries and decryption queries are valid. So  $R_2$  will not abort during the simulation, the possibility of perfect simulation is 1. From these we can conclude that Rival  $R_1$ 's view is identical to its view

 $R_1$  we have that  $|Pr[c = c'] - 1/2| \ge \epsilon(k)$ , thereby  $R_2$ has at least advantage  $\epsilon(k)$  against beta cryptosystem. This proves theorem 5.0.2 and terminates the proof.

### Performance Comparison of 6 Other ID-based Cryptographic Schemes

In this section, we have discussed four most wide-used ID-based encryption schemes and compared their performance. These four ID-based cryptographic schemes are: Selective-ID Secure ID-based cryptosystem without Random Oracles [3], Boneh-Franklin ID-based cryptosystem [6], Cocks ID-based cryptosystem [7], Authenticated ID-based cryptosystem [13], and our proposed ID-based beta cryptosystem. These schemes have different performance on server for evaluating Encrypt algorithm performance, decryption algorithm performance, and computational cost. Notations used in this computation are as follows: P = airing operation, M = Modular multiplication, e = Exponentiation in G, m =Scalar or Point Multiplication in G, x = XOR operation, h = Hashing, a = addition modulo, i = inverses modulo, J = Jacobisymbol and  $C(\gamma) =$ Computation cost of operation  $\gamma$ .



Figure 1: Computational cost

Based on our observation of Figure 1, we have observed that proposed ID-based beta cryptosystem has a better performance than other four schemes [3, 6, 7, 13]in encryption and decryption algorithms. Our proposed scheme is faster than schemes [3, 6, 7, 13] in two aspects. First, our proposed scheme needs no pairing computation in encrypt algorithm and decryption algorithm, because  $\tilde{e}(P_1, P_2)$  can be pre-computed. Secondly, in the operation of mapping an identity to an element in  $G_1$  or  $G_2$ , the map-to-point algorithm used by scheme [6] and scheme [3] is not required because simple hash function is used in our scheme to map an identifier to an element in  $Z_N^*$ . Our proposed scheme is faster than scheme [7] in the factual attack. By the definition of algorithm in one aspect. The size of ciphertext is very large and

consists of two elements of  $Z_N$  per bit of the message arithm problem and integer factorization problem-based but the size of our proposed scheme is smaller than system. scheme [7] and consists of an element of  $Z_N^*$  per bit of the message.



Figure 2: Total computational cost

Also, we evaluated the total computational cost of the four schemes [3, 6, 7, 13] and proposed scheme in Figure 2. We found that the computation cost of scheme [3] is near about the scheme [13] and the computation cost of scheme [7] is near about the scheme [6] and the computation cost of our proposed is much less to other four schemes and half of scheme [13]. As we know that in the Extract algorithm of scheme [6] and scheme [13], an identity string is mapped to a point on an elliptic curve and the corresponding private key is computed by multiplying the mapped point with the master key of public key generator (PKG) and Extract algorithm of our proposed scheme requires much simpler hashing than the schemes [6, 7, 13]. Hence the computational cost will reduce and therefore improves performance.

#### 7 Conclusion

In this article, we deals with new mechanisms for IDbased beta cryptographic scheme, whose unforgeability can be reduced to the hardness of the generalized discrete logarithm problem and integer factorization problem over multiplicative group, which are a fundamental intractable problems in cryptography. It is selective identity adaptive chosen ciphertext security (INDsID-CCA) under assumption of generalized discrete logarithm problem and integer factorization problem over multiplicative group in random oracle. This scheme is fast than Boneh and Franklin-ID-based cryptographic scheme, Cocks- ID-based cryptographic scheme, Authenticated ID-based cryptographic scheme, Selective-ID Secure IDbased cryptographic scheme and having very low computational cost. Therefore, our new scheme is more practical and has the same security as the original discrete log-

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