# A Provably Password Authenticated Key Exchange Scheme Based on Chaotic Maps in Different Realm

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# Abstract

Until now, the overwhelming majority of passwordauthenticated key agreement protocols using chaotic maps are based on three architectures (client/server, two clients/server and multi-server) and four security models (heuristic security, random oracle, ideal cipher and standard model). However, with rapid changes in the modern communication environment such as wireless mesh networks and cloud storing, it is necessary to put forward a kind more flexible and general architecture to adapt it. So, in our paper, we firstly propose a provable secure twoparty in two-realm key agreement protocol using chaotic maps in the standard model. Our proposed protocol is more general and it is easy to expand to many other forms, such as three-party or N-party in different realms. The new protocol resists dictionary attacks mounted by either passive or active network intruders, allowing, in principle, even weak password phrases to be used safely. It also offers perfect forward secrecy, which protects past sessions and passwords against future compromises. Finally, we give the security proof in the standard model and the efficiency analysis of our proposed scheme.

Keywords: Chaotic maps, different realms, key exchange, mutual authentication

# 1 Introduction

Nowadays, chaos theory has widely used to cryptography. Chaotic system has numerous advantages, such as extremely sensitive to initial parameters, unpredictability, boundness, etc. Meanwhile, chaotic sequence generated by chaotic system has the properties of non-periodicity and pseudo-randomness. In a word, chaos theory and chaotic system have exploited a new way for cryptography.

In 1998, Baptista [1] firstly connects cryptography with

chaos theory. As a fundamental cryptographic primitive, key agreement protocol allows two or more parties to agree on shared keys which will be used to protect their later communication. Then, combining chaos theory and key agreement primitive, many authenticated key exchange (AKE) protocols [7, 8, 12, 16, 21, 23, 24, 25] have been proposed. The literature [25] firstly proposed a new one-way authenticated key agreement scheme (OWAKE) based on chaotic maps with multi-server architecture. The OWAKE scheme is widely used to no need for mutual authentication environment on Internet, such as readersto-journalists model and patient-to-expert model. Using the chaotic maps, the literature [24] firstly proposed a new multiple servers to server architecture (MSTSA) to solve the problems caused by centralized architecture, such as multi-server architecture with the registration center (RC). The core ideas of the proposed scheme are the symmetry (or called peer to peer) in the servers side and the transparency for the clients side. In brief, based on chaotic maps, there were many AKE protocols from functionality aspect, or from efficiency aspect, or from security aspect, or from architecture aspect to improve the AKE protocols.

However it is quite unrealistic that two clients trying to communicate with each other are registered on the same server. In the real situation with distributed applications, an authentication setting usually occurs such that two clients are registered in different servers. For example, from a user's point of view in a mobile computing environment, a secure end-to-end channel between one mobile user in cell A and another user in cell B may be a primary concern. Additionally, the end-to-end security service minimizes the interferences from the operator controlled network components. Over the past years, many protocols based on the different password authentication (DPWA) model have been presented in the cross-realm setting and some of them have been easily broken and subsequently modified [2, 5, 9, 13, 15]. Byun et al. first proposed a Client-to-Client Password-Authenticated Key Exchange (C2C-PAKE) in the cross-realm setting where two clients are in two different realms and hence two servers involved [2]. Unfortunately, the scheme was found to be flawed. Chen first pointed out that one malicious server in the cross-realm setting could mount a dictionary attack to obtain the password of a client who belongs to the other realm [5]. In [15], Wang et al. showed dictionary attacks by a malicious server on the same protocol. Kim et al. [9] pointed out that the protocol was susceptible to Dening-Sacco attacks [6], and they also proposed an improved C2C-PAKE protocol. However, very recently, Phan and Goi suggested two unknown key share attacks on the improved C2C-PAKE protocol. They presented countermeasures in [13]. Up until now, several countermeasures to protect the attacks on the C2C-PAKE protocol have been presented in [2, 5, 9, 13, 15]. Recently Byun [3] presented an efficient C2C-PAKE protocol and proved it is secure under decisional Diffie-Hellman assumption in the ideal cipher and random oracle models. But most of the presented protocols were susceptible to Off-line Password Guessing Attacks with Server Compromise. The main reason [17, 22] is that there is a need for the password to encrypt or decrypt some information during the protocol process. This implies that the server has to store the plaintext password. So the password verification information in the server obtained by the attacker may mount an Off-line Password Guessing Attacks.

Based on the chaotic maps, we believe the more general architecture should be involved in AKE protocols. So we propose the first two-party in two-realm key exchange protocol using chaotic maps in standard model.

The rest of the paper is organized as follows: Some preliminaries are given in Section 2. Next, a novel chaotic maps problem is described in Section 3. Then, the noninteractive twin chaotic maps-key exchange protocol is given in Section 4. The Security of our proposed protocol is given in Section 5. The efficiency analysis of our proposed protocol and some feasible applications are given in Section 6. This paper is finally concluded in Section 7.

## 2 Preliminaries

## 2.1 One-way Hash Function and Pseudorandom Function Ensembles

There are four main properties in a secure cryptographic one-way hash function  $h: a \rightarrow b$ :

- The function h takes a message of arbitrary length as the input and produces a message digest of fixedlength as the output;
- The function h is one-way in the sense that given a, it is easy to compute h (a) = b. However, given b, it is hard to compute h<sup>-1</sup> (b) = a;
- 3) Given a, it is computationally infeasible to find a' such that  $a' \neq a$ , but h(a') = h(a);

4) It is computationally infeasible to find any pair a, a' such that  $a' \neq a$ , but h(a') = h(a).

Pseudo-random function ensembles:

If a function ensemble  $F = \{F_n\}_{n \in \mathbb{N}}$  is pseudorandom [14], then for every probabilistic polynomial oracle  $\mathcal{A}$  and all large enough n, we have that:

$$\mathcal{A}^{G_n}(1^n) = 1]| < \varepsilon(n)$$

where  $G = \{G_n\}_{n \in N}$  is a uniformly distributed function ensemble,  $\varepsilon(n)$  is a negligible function,  $Adv^F = \max_{\mathcal{A}} \{Adv^F(\mathcal{A})\}$  denotes all oracle  $\mathcal{A}$ , and  $Adv^F(\mathcal{A})$  represents the accessible maximum.

#### 2.2 Symmetric Encryption

A symmetric encryption scheme  $E_k(Kgen, E, D)$  consists of three algorithms as follows:

- 1) Randomized Key Generation Algorithm Kgen: it returns a key k drawn from the key space  $Keys(E_k)$  at random.
- 2) Encryption Algorithm E: it takes the key  $k \in Keys(E_k)$  and a plaintext  $M \in \{0,1\}^*$  as the inputs and outputs a ciphertext  $C \in \{0,1\}^*$ . So it can be written  $C = E_k(M)$ .
- 3) Decryption Algorithm D:it takes the key  $k \in Keys(E_k)$  and a ciphertext  $C \in \{0,1\}^*$  as the inputs and outputs a plaintext  $M \in \{0,1\}^*$ . So it can be written  $M = D_k(C)$ .

## 2.3 Definition and Hard Problems of Chebyshev Chaotic Maps

Let *n* be an integer and let *x* be a variable with the interval [-1, 1]. The Chebyshev polynomial  $T_n(x)$ :  $[-1, 1] \rightarrow$ [-1, 1] is defined as  $T_n(x) = \cos(n\cos^{-1}(x))$  [16]. Chebyshev polynomial map  $T_n$ :  $R \rightarrow R$  of degree *n* is defined using the following recurrent relation:

$$T_n(x) = 2xT_{n-1}(x) - T_{n-2}(x),$$

where  $n \ge 2, T_0(x) = 1$ , and  $T_1(x) = x$ . The first few Chebyshev polynomials are:

$$T_2(x) = 2x^2 - 1,$$
  

$$T_3(x) = 4x^3 - 3x,$$
  

$$T_4(x) = 8x^4 - 8x^2 + 1,$$
  
...

One of the most important properties is that Chebyshev polynomials are the so-called semi-group property which establishes that

$$T_r(T_s(x)) = T_{rs}(x).$$

An immediate consequence of this property is that Chebyshev polynomials commute under composition

$$T_r(T_s(x)) = T_s(T_r(x)).$$

In order to enhance the security, Zhang [21] proved that semi-group property holds for Chebyshev polynomials defined on interval  $(-\infty, +\infty)$ . The enhanced Chebyshev polynomials are used in the proposed protocol:

$$T_n(x) = (2xT_{n-1}(x) - T_{n-2}(x)) \pmod{N}$$

where  $n \ge 2$ ,  $x \in (-\infty, +\infty)$ , and N is a large prime number. Obviously,

$$T_{rs}(x) = T_r(T_s(x)) = T_s(T_r(x)).$$

**Definition 1.** (Semi-group property) Semi-group property of Chebyshev polynomials:

$$T_{rs}(x) = T_r(T_s(x)) = \cos(r\cos^{-1}(s\cos^{-1}(x))) = \cos(rs\cos^{-1}(x)) = T_s(T_r(x)) = T_{sr}(x),$$

where r and s are positive integer and  $x \in [-1, 1]$ .

**Definition 2.** (Chaotic Maps-Based Discrete Logarithm (CDL) problem) Given x and y, it is intractable to find the integer s, such that  $T_s(x) = y$ . The probability that a polynomial time-bounded algorithm  $\mathcal{A}$  can solve the CDL problem is defined as  $Adv_{\mathcal{A}}^{CDL}(p) = \Pr[\mathcal{A}(x,y) = r : r \in \mathbb{Z}_p^*, y = T_r(x) \mod p].$ 

**Definition 3.** (CDL assumption) For any probabilistic polynomial time-bounded algorithm  $\mathcal{A}$ ,  $Adv_{\mathcal{A}}^{CDL}(p)$  is negligible, that is,  $Adv_{\mathcal{A}}^{CDL}(p) \leq \varepsilon$ , for some negligible function  $\varepsilon$ .

**Definition 4.** (Chaotic Maps-Based Diffie-Hellman (CDH) problem) Given x,  $T_r(x)$  and  $T_s(x)$ , it is intractable to find  $T_{rs}(x)$ . The probability that a polynomial time-bounded algorithm  $\mathcal{A}$  can solve the CDH problem is defined as  $Adv_{\mathcal{A}}^{CDH}(p) = \Pr[\mathcal{A}(x, T_r(x) \mod p, T_s(x) \mod p) = T_{rs}(x) \mod p : r, s \in \mathbb{Z}_p^*].$ 

**Definition 5.** (CDH assumption) For any probabilistic polynomial time-bounded algorithm  $\mathcal{A}$ ,  $Adv_{\mathcal{A}}^{CDH}(p)$  is negligible, that is,  $Adv_{\mathcal{A}}^{CDH}(p) \leq \varepsilon$ , for some negligible function  $\varepsilon$ .

## 2.4 Definition and Properties of Chebyshev Chaotic Maps

**Definition 6.** [7, 8]  $f: J \to J$  is said to be topologically transitive if for any pair of open sets  $U, V \subset J$ , there exists k > 0 such that  $f^k(U) \cap V \neq \phi$ .

**Definition 7.**  $f: J \to J$  has sensitive dependence on initial conditions if there exists  $\delta > 0$  such that for any  $x \in J$  and any neighborhood N of x, there exist  $y \in N$ and  $n \ge 0$  such that  $|f^n(x) - f^n(y)| > \delta$ .

**Definition 8.** Let V be a set, then  $f: V \to V$  is said to be chaotic on V if

- 1) f has sensitive dependence on initial conditions.
- 2) f s topologically transitive.
- 3) Periodic points are dense in V.

**Definition 9.** Let  $f : A \to A$ ,  $f : B \to B$  be two maps, if there exists a continuous surjection  $h : A \to B$  such that  $h \cdot g = g \cdot h$ , we say that these two maps f and g are topologically semi-conjugate.

**Theorem 1.** A non-zero polynomial is the  $n^{th}$  Chebyshev polynomial or its constant times iff the nonzero polynomial is the root of the differential equation

$$(1 - x^2) y'' - xy' + n^2 y = 0 \ (n \in \mathbf{Z}_+)$$

**Lemma 1.** If  $f : A \to A$ ,  $f : B \to B$  are topologically semi-conjugate,

- When p is the periodic point of f, then h(p) is the periodic point of g;
- When the periodic point of f is dense in A, the periodic point of g is dense in B, where h is the topologically semi-conjugate between f and g.

**Lemma 2.** Assume  $f : A \to B$  is a map,  $A_0, A_1 \subset A$ , then  $f(A_0 \cap A_1) \subset f(A_0) \cap f(A_1)$ .

**Lemma 3.** When  $f : A \to A$  is topologically transitive,  $g : B \to B$  is topologically semi-conjugate f via h, then g is topologically transitive.

**Lemma 4.** Let  $R: S' \to S'$  be a map of the circle into itself, then  $R(\theta) = n\theta$  ( $n \in \mathbb{Z}, n \ge 2$ ) is chaotic, where  $\theta$  is the radian value.

The concrete proof of chaotic properties can be found in the literature [8] and the enhanced properties of Chebyshev polynomials that defined on interval  $(-\infty, +\infty)$  still have the semi-group property (see [21]).

# 3 The Proposed Protocol

In this section, under the two-realm environment for two client with two servers, a chaotic maps-based authentication key agreement scheme is proposed which consists of three phases: registration phase, authentication key agreement phase and password update phase.

#### 3.1 Notations

In this section, any server *i* has its identity  $ID_{S_i}$  and public key  $(x, T_{K_i}(x))$  and a secret key  $K_i$  based on Chebyshev chaotic maps, a secure one-way hash function  $H(\cdot)$ , a pseudo-random function *F*, and a pair of secure symmetric encryption/decryption functions  $E_K()/D_K()$  with key *K*. The concrete notations used hereafter are shown in Table1.

Table 1: Notations

Symbol	Definition
$ID_A, ID_B, ID_{Session}$	The identity of Alice, Bob and the session, respectively;
$S_i, ID_{S_i}$	The $i^{th}$ server; The identity of the $i^{th}$ server, respectively;
$a, b, S_a, S_b, S_{aa}, S_{bb}$	Nonces;
$(x, T_k(x))$	Public key based on Chebyshev chaotic maps;
K	Secret key based on Chebyshev chaotic maps;
$E_k(\cdot)/D_k(\cdot)$	A pair of secure symmetric encryption/decryption functions with the key $K$ ;
H	A secure one-way hash function;
F	Pseudo-random function;
	Concatenation operation.



Figure 1: A authenticated expert registration phase

#### 3.2 Registration Phase

Concerning the fact that the proposed scheme mainly relies on the design of Chebyshev chaotic maps-based in two-realm architecture, it is assumed that Alice can register at the serverA in the same realm by secure channel. The same assumption can be set up for servers. Figure 1 illustrates the server registration phase.

- **Step 1.** When a user Alice wants to be a new legal user, she chooses her identity  $ID_A$  and password  $PW_A$  and sends  $\{ID_A, HPW_A\}$  to the server via a secure channel.
- **Step 2.** Upon receiving  $\{ID_A, HPW_A\}$  from the Alice, the server A stores  $\{ID_A, HPW_A\}$  in a secure way.

#### 3.3 Authenticated Key Agreement Phase

This concrete process is presented in Figure 2.

- **Step 1.** If Alice wishes to consult some personal issues establish with Bob in a secure way, but they are in different realm. Alice will choose a large and random a. Then the device of Alice will compute  $T_a(x), C_{A_1} = T_a(x)T_{HPW_A}T_{K_A}(x)$  and  $Mac_{AS} =$  $F_{T_aT_{K_A}(x)}(ID_{Session}||C_{A_1})$ . After that, Alice sends  $ID_A, ID_B, C_{A_1}, Mac_{AS}$  to **Server**<sub>A</sub> where she registers on (The same way for Bob).
- **Step 2.** After receiving the message  $ID_A$ ,  $ID_B$ ,  $C_{A_1}$ ,  $Mac_{AS}$  from Alice, **Server**<sub>A</sub> will do the following tasks:
  - 1) Server<sub>A</sub> uses  $HPW_A$  to compute  $T_a(x) = C_{A_1}/T_{HPW_A}T_{K_A}(x)$ .

- 2) Server<sub>A</sub> examines whether is valid in terms of the  $(ID_{Session}||C_{A_1})$ .
- 3) Server<sub>A</sub> selects a large and random integer  $S_a$ to compute  $T_{S_a}(x)$ ,  $C_{A_2} = T_a(x)T_{S_a}T_{K_B}(x)$ ,  $Mac_{SAB} = F_{T_aT_{K_B}(x)}(ID_{Session}||C_{A_2})$  and sends  $ID_A, ID_B, C_{A_2}, T_{S_a}(x), Mac_{SAB}$  to Server<sub>B</sub> (The same way for Server<sub>B</sub>).
- **Step 3.** After receiving the message  $ID_A$ ,  $ID_B$ ,  $C_{A_2}$ ,  $T_{S_a}(x)$ ,  $Mac_{SAB}$  from **Server**<sub>A</sub>, **Server**<sub>B</sub> will uses  $K_B$  to compute  $T_a(x) = C_{A_2}/T_{S_a}T_{K_B}(x) =$   $C_{A_2}/T_{K_B}T_{S_a}(x)$ . Then **Server**<sub>B</sub> examines whether  $Mac_{SAB} = F_{T_aT_{K_B}(x)}(ID_{Session}||C_{A_2})$  is valid in terms of the  $(ID_{Session}||C_{A_2})$ . **Server**<sub>B</sub> selects a large and random integer  $S_{bb}$  and computes  $T_{S_{bb}}(x)$ ,  $C_{A_3} = T_{S_{bb}}T_{HPW_B}T_a(x)$ ,  $Mac_{SB} = F_{T_aT_b(x)}(ID_{Session}||C_{A_3})$  and sends  $ID_A, ID_B, C_{A_3}, T_{S_{bb}}(x), Mac_{SB}$  to Bob (The same way for **Server**<sub>A</sub>).
- **Step 4.** After receiving the message  $ID_A$ ,  $ID_B$ ,  $C_{A_3}$ ,  $T_{S_{bb}}(x)$ ,  $Mac_{SB}$ , Bob uses  $HPW_B$  to compute

$$T_{a}(x) = C_{A_{3}}/T_{S_{bb}}T_{HPW_{B}}(x)$$
$$= C_{A_{3}}/T_{HPW_{B}}T_{S_{bb}}(x).$$

Then Bob examines whether  $Mac_{SB} = F_{T_{HPW_B}T_{S_{bb}}}(ID_{Session}||C_{A_3})$  is valid in terms of the  $(ID_{Session}||C_{A_3})$ . If holds, and the session key is  $SK = F_{T_bT_a(x)}$  (1).(The same way for Alice). If any authenticated process does not pass, the protocol will be terminated immediately.



Figure 2: Authenticated key agreement phase



Figure 3: Password update phase

#### 3.4 Password Update Phase

This concrete process is presented in the following Figure 3.

- Step 1. If Alice wishes to update her password with Server<sub>A</sub>, Alice will choose a new memorable password  $PW'_A$ . Then the device of Alice will compute  $HPW'_A = H\left(ID_A||PW'_A||T_{K_A}(x)\right), T_{HPW'_A}(x),$   $C_{A_1} = T_{HPW'_A}(x)T_{HPW_A}T_{K_A}(x)$  and  $Mac_{AS} =$   $F_{T_{HPW'_A}T_{K_A}(x)}(ID_A||ID_{S_A}||C_{A_1})$ . After that, Alice sends  $ID_A$ ,  $ID_{S_A}$ ,  $C_{A_1}$ ,  $Mac_{AS}$  to Server<sub>A</sub> where she registers on.
- **Step 2.** After receiving the message  $ID_A$ ,  $ID_{S_A}$ ,  $C_{A_1}$ ,  $Mac_{AS}$  from Alice, **Server**<sub>A</sub> will do the following tasks:
  - 1) Server<sub>A</sub> uses  $HPW_A$  to compute  $T_{HPW'_A}(x) = C_{A_1}/T_{HPW_A}T_{K_A}(x)$ .
  - 2) Server<sub>A</sub> examines whether  $Mac_{AS} = F_{T_{HPW'_{A}}T_{K_{A}}(x)}(ID_{A}||ID_{S_{A}}||C_{A_{1}})$  is valid in terms of the  $(ID_{A}||ID_{S_{A}}||C_{A_{1}})$ .
  - 3) If holds, **Server**<sub>A</sub> computes  $Mac_{SA} = F_{T_{HPW_A}T_{HPW'_A}(x)}(ID_A||ID_{S_A}||T_a(x))$  and sends  $ID_A, ID_{S_A}, Mac_{SA}$  to Alice. Replaces the  $HPW_A$  by  $HPW'_A$ .
- **Step 3.** After receiving the message  $ID_A$ ,  $ID_{S_A}$ ,  $Mac_{SA}$  from **Server**<sub>A</sub>, Alice will uses  $HPW_A$ ,  $HPW'_A$  to compute  $Mac'_{SA} =$   $F_{T_{HPW_A}T_{HPW'_A}(x)}(ID_A||ID_{S_A}||T_{HPW'_A}(x))$  to verify  $Mac_{SA}$ . If holds, Alice replaces the  $HPW_A$  by  $HPW'_A$ .

# 4 Security Consideration

The section a theorem concerning the semantic security of our proposed protocol is given.

#### 4.1 Security Model

We recall the protocol syntax and communication model [4, 11, 19]. The basic descriptions and some queries are shown in Table 2.

#### 4.2 Security Proof

**Theorem 2.** Let  $\Gamma$  be a two-party in two-realm PAKE protocol described in Figure 2. Let  $F : \{0,1\}^n \to \{0,1\}^{l(n)}$ be a pseudo-random function ensembles. Because the DDH assumption holds in enhanced Chebyshev chaotic maps, then

$$Adv_{x,T_{u},F}^{2P2RPAKE}(t,R) \le \frac{2q_e^2 + 3q_s^2 + 2(q_e + q_s)^2}{N_1}$$

 $+2(q_e+q_s)Adv^F+2(\min\{q_e,q_r\}+\min\{q_s,q_r\})Adv^F$ 

$$+2(q_e+q_s)Adv_{x,T_u}^{DDH} + \frac{q_s}{2^{n-1}} + \frac{(q_e+q_s)^2}{N_1}\frac{q_s}{N_1}$$

where n is a safe parameter,  $l(\cdot)$  is a function that can be computed in polynomial time.  $N_1$  is a large prime number,  $u, T_u(x)$  are the private and public keys of the server,  $q_e, q_r, q_s$  represent the maximum number of Execute and Test that the adversary can inquire, and queries from Send-Client and Send-Server, N is the password dictionary D's size,  $Adv_{x,T_u}^{DDH}$  represents the probability of breaking the DDH hypothesis, and  $Adv^F$  denotes the probability of breaking the pseudo-random function ensembles.

In order to make the security proof simple, we firstly point out the differences between the literature [19] and our proposed protocol. Then we give the differences between the literature [11] and our proposed protocol. Finally, we will get Theorem 2.

1) The differences between the literature [19] and our proposed protocol. Using enhanced Chebyshev chaotic maps to replace ElGamal encryption. To be specific,  $g^{x_2}, rg^{x_1}, Zg^{x_1}$  and  $g^{x_1}h^{x_2}$ in the literature [19] should be replaced by  $T_{x_2}(x), rT_{x_1}(x), ZT_{x_1}(x)$  and  $T_{x_1}(x)T_{x_2}(h)$ , respectively.

The birthday paradox should be used to replace the probability of random events when the event collision occurs. According to the birthday paradox, the probability of collisions in output  $T_n(x)$  is at most  $q_s^2/2N_1$ , where  $q_s$  denotes the maximum number of Send-Client and Send-Server queries.

According to the birthday paradox, the probability of collisions in output  $T_n(x)$  is at most  $(q_s + q_e)^2/2N_1$ , where  $q_s$  denotes the maximum number of Send-Client and Send-Server queries,  $q_e$  denotes the maximum number of Execute queries. Hence, the probability of distinguishing  $Mac_{**}$  with random integers is  $(q_s + q_e)^2/2N_1$ .

2) The differences between the literature [11] and our proposed protocol. We convert the low entropy secret password PW to high entropy cryptography key by a one-way hash function  $HPW_A =$  $H(ID_A||PW_A||T_{K_A}(x))$  which is more secure way than the literature [11] only stored password in the server database.

Different architecture. Our proposed protocol sets up in different realm and the two-party has different password with his/her service server. That means one Send-Client query will test two passwords in the same set. So in our protocol, when relating with N (N is the password dictionary D size), and it is the same with the literature [11].

**Round 1.** Our proposed protocol has one more  $Mac_{**}$  for each party, so there is must have one more  $(q_s + q_e)^2/2N_1$ .

Table 2: Descriptions the model and the queries

Symbol	Definition						
Parties $P_1, \dots, P_n$	Modelled by probabilistic Turing machines. Two non-empty sets: User, the set of						
or $(C_1, \dots, C_n, S_1,$	all clients, and Server, the set of trusted servers constitute the participants in our						
$\cdots, S_n$ )	2P2RPAKE protocol.						
Adversary $\Lambda$	A probabilistic Turing machine which controls all communication, with the excep-						
	tion that the adversary cannot inject or modify messages (except for messages from						
	corrupted parties or sessions), and any message may be delivered at most once.						
Sessions matching	If the outgoing messages of one are the incoming messages of the other.						
$\prod_{U_1}^{i}, \ pid_{U_1}^{i}, \ sid_{U_1}^{i},$	Denote participant $U_1$ 's instance <i>i</i> , who is involved with a partner participant $U_2$						
$\prod_{U_2}^{j}$ , $pid_{U_2}^{j}$ , $sid_{U_2}^{j}$	in a session. $\prod_{U_1}^i$ has the parner identification $pid_{U_1}^i$ and the session identification						
	$sid_{U_1}^i$ . The same means for $\prod_{U_2}^j$ , $pid_{U_2}^j$ , $sid_{U_2}^j$ .						
Execute $(\prod_{IL}^{i}, S^{i})$	This query returns the messages that were communicated in the course of an honest						
$S_j, \prod_{U_2}^j)$	execution of the protocol among $\prod_{U_1}^i, S^i, S_j, \prod_{U_2}^j$ .						
Send-Client $(\prod_{U_1}^i)$	This query returns the message that client instance $\prod_{U_{k}}^{i}$ , which would generate						
(k = 1, 2), m)	upon receipt of message $m$ .						
Send-Server $(S^k)$	This query returns the message that server instance $S^k$ would generate upon receipt						
(k = 1, 2), m)	of message $m$ . When receiving a fabricated message by an adversary, the server						
	instance $S^k$ responds in the manner prescribed by the protocol.						
Corrupt $(U_k \ (k = 1, 2))$	This query returns the session key of the client instance $U_k$ $(k = 1, 2)$ .						
Reveal $(\prod_{i=1}^{i} (k = 1))$	This query returns the password and the states of all instances of $U_k$ ( $k = 1, 2$ ) only						
(1,2))	when it is defined.						
Test $(\prod_{U_i}^i (k) =$	This query allows the adversary to be issued at any stage to a completed, fresh,						
(1,2))	unexpired session. A bit $b$ is then picked randomly. If $b = 0$ , the test oracle reveals						
	the session key, and if $b = 1$ , it generates a random value in the key space. The						
	adversary $\Lambda$ can then continue to issue queries as desired, with the exception that						
	It cannot expose the test session.						
Partnering	We say two instances $\prod_{U_1}^{i}$ and $\prod_{U_2}^{j}$ are partners iff: (a) They are successfully						
Partnering	We say two instances $\prod_{U_1}^{i}$ and $\prod_{U_2}^{j}$ are partners iff: (a) They are successfully accepted; (b) $sid_{U_1}^{i} = sid_{U_2}^{j}$ ; (c) $pid$ for $\prod_{U_1}^{i}$ is $\prod_{U_2}^{j}$ and vice versa; (d) No instance						
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Partnering Freshness	It cannot expose the test session. We say two instances $\prod_{U_1}^i$ and $\prod_{U_2}^j$ are partners iff: (a) They are successfully accepted; (b) $sid_{U_1}^i = sid_{U_2}^j$ ; (c) $pid$ for $\prod_{U_1}^i$ is $\prod_{U_2}^j$ and vice versa; (d) No instance other than $\prod_{U_1}^i$ and $\prod_{U_2}^j$ accepts with a $pid$ equal to $\prod_{U_1}^i$ or $\prod_{U_2}^j$ . Let $\prod_{U_1,U_2,S_1,S_2}^i$ be a completed session by a party $U_1$ with some other party $U_2$ , and $\prod_{U_2,U_1,S_2,S_1}^j$ be the matching session to $\prod_{U_1,U_2,S_1,S_2}^i$ . We say that the session $\prod_{U_1,U_2,S_1,S_2}^i$ is fresh if $U_1$ and $U_2$ in session $\prod_{U_1,U_2,S_1,S_2}^i$ and the matching session $\prod_{U_2,U_1,S_2,S_1}^j$ are honest and the following conditions hold: (a) $\prod_{U_1,U_2,S_1,S_2}^i$ has ac- cepted the request to establish a session key. (b) $\prod_{U_1,U_2,S_1,S_2}^i$ has not been revealed. (c) No matching conversation $\prod_{U_2,U_1,S_2,S_1}^j$ of $\prod_{U_1,U_2,S_1,S_2}^i$ has been revealed. (d)						
Partnering Freshness	It cannot expose the test session. We say two instances $\prod_{U_1}^i$ and $\prod_{U_2}^j$ are partners iff: (a) They are successfully accepted; (b) $sid_{U_1}^i = sid_{U_2}^j$ ; (c) $pid$ for $\prod_{U_1}^i$ is $\prod_{U_2}^j$ and vice versa; (d) No instance other than $\prod_{U_1}^i$ and $\prod_{U_2}^j$ accepts with a $pid$ equal to $\prod_{U_1}^i$ or $\prod_{U_2}^j$ . Let $\prod_{U_1,U_2,S_1,S_2}^i$ be a completed session by a party $U_1$ with some other party $U_2$ , and $\prod_{U_2,U_1,S_2,S_1}^j$ be the matching session to $\prod_{U_1,U_2,S_1,S_2}^i$ . We say that the session $\prod_{U_2,U_1,S_2,S_1}^i$ is fresh if $U_1$ and $U_2$ in session $\prod_{U_1,U_2,S_1,S_2}^i$ and the matching session $\prod_{U_2,U_1,S_2,S_1}^j$ are honest and the following conditions hold: (a) $\prod_{U_1,U_2,S_1,S_2}^i$ has ac- cepted the request to establish a session key. (b) $\prod_{U_1,U_2,S_1,S_2}^i$ has not been revealed. (c) No matching conversation $\prod_{U_2,U_1,S_2,S_1}^j$ of $\prod_{U_1,U_2,S_1,S_2}^i$ has been revealed. (d) $U_2, S$ has not been corrupted. (e) The adversary asks neither Send-Client ( $\prod_{U_1}^i, m$ )						

Model KP FS UDOD UKS PCI OFD MA AR Our protocol S Yes Yes C2S2Yes Yes Yes Yes Yes Yang and Cao's protocol [19]  $\mathbf{S}$ Yes Yes C2SYes Yes Yes Yes Yes  $\mathbf{S}$ Lai et al.'s protocol [11] Yes C2SYes Yes Yes Yes Yes Yes Yoon-Jeon's protocol [20] Ν No Yes C2SNo Yes No No No Xie et al.'s protocol [18] Ν Yes C2SYes Yes Yes No No Yes Ν C2SLee et al.'s protocol [12] Yes Yes No No Yes Yes No

Table 3: Security comparison existing protocols for 3PAKE based on Chebyshev chaotic maps and our protocol

S standard model, N nonstandard model, KP key privacy, MA mutual authentication, AR architecture, C2S client-to-server, C2S2 Two-client-two-server, FS forward security, UDOD security against undetectable on-line dictionary attack, UKS security against unknown key-share attack, PCI security against password compromised impersonation attack, OFD security against off-line dictionary attack.

- Round 2. The only difference between the literature [11] and our proposed protocol is that one server changes into two servers. So that brings about two points changed:
  - 1) There are two more  $Mac_{**}$ , so the probability of distinguishing  $Mac_{**}$  with random integers is  $(q_s + q_e)^2/2N_1$ .
  - 2) According to the birthday paradox, there are two more  $T_n(x)$ , so the probability of collisions in output  $T_n(x)$  is at most  $q_s^2/N_1$ .
- Round 3. It is the same with the literature [11]. The detailed descriptions of these games and lemmas are analogous to those in literature [11], with the differences discussed above, and therefore, they are omitted.

**Theorem 3.** Our proposed two-realm PAKE protocol ensures key privacy against the server based on the fact that DDH assumption holds in the enhanced Chebyshev chaotic maps and F is a secure pseudo-random function ensemble, and

$$Adv_D^{k_p}(\Lambda_{k_p}) \le 4q_s Adv_{x,T_u}^{DDH} + 2q_e Adv^F$$

where  $q_e$  and  $q_s$  denote the maximum number of queries to the oracle Execute and Send-Client.

The proof of Theorem 3 is similar to that of Theorem 5.2 in [19] and Theorem 3 in [11]. The difference between our proposed protocol and the literature [19] is that we just replace the enhanced Chebyshev chaotic map values with the ElGamal discrete logarithm values. The difference between our proposed protocol and the literature [11] is that our proposed protocol is designed in different realm with different password, so some changed details can be described in Section 4.2.

Next, from the Table 3, we can see that the proposed scheme can provide secure session key agreement, perfect forward secrecy and so on. As a result, the proposed scheme is more secure and has much functionality compared with the recent related scheme.

## 5 Efficiency Analysis

# 5.1 The Comparisons Between Our Scheme and the Literature in Different Realms with Different Algorithms

Compared to RSA and ECC, Chebyshev polynomial computation problem offers smaller key sizes, faster computation, as well as memory, energy and bandwidth savings. In our proposed protocol, no time-consuming modular exponentiation and scalar multiplication on elliptic curves are needed. However, Wang [16] proposed several methods to solve the Chebyshev polynomial computation problem.

To be more precise, on an Intel Pentium4 2600 MHz processor with 1024 MB RAM, where n and p are 1024 bits long, the computational time of a one-way hashing operation, a symmetric encryption/decryption operation, an elliptic curve point multiplication operation and Chebyshev polynomial operation is 0.0005s, 0.0087s, 0.063075s and 0.02102s separately [10]. Moreover, the computational cost of XOR operation could be ignored when compared with other operations.

For simplicity, the literatures [3, 6, 13, 15] in the different realms architecture, we omit the comparisons table detailedly. The reason is that our proposed protocol are mainly based on chaotic maps algorithms which is more efficient than the other algorithms, such as RSA and ECC, in the literatures [3, 10, 13, 15].

## 5.2 The Comparisons Between Our Scheme and the Literature with the Same Algorithms

Table 4 shows performance comparisons between our proposed scheme and the literature of [11, 12, 18, 19, 11, 20] in three-party architecture with chaotic maps.

R	R	N	Pł	КE	Sk	КE	ſ	[	
	(A/B/S)		(A/B/S)		(A/B/S)		(A/B/S)		
	$(A/B/S_A/S_B)$		$(A/B/S_A/S_B)$		$(A/B/S_A/S_B)$		$(A/B/S_A/S_B)$		
Our protocol 3		1/1/1/1		0/0/2/2		0/0/0/0		2/2/4/4	
4	2/2/3		0/0/1		0/0/1		0/0/0		
4	2/2/3		0/0/1		0/0/1		6/6/10		
5	2/1/0		2/2/0		1/1/1		2/2/0		
6	1/1/1		2/2/0		3/3/0		3/3/2		
5	1/1/1		2/2/0		4/4	4/4/0		3/2	
			H		D		F		
The others			B/S)	(A/B/S)		(A/B/S)			
Our protocol			$(A/B/S_A/S_B)$		$(A/B/S_A/S_B)$		$(A/B/S_A/S_B)$		
Our protocol			0/0/0/0		0/0/0/0		2/2/4/4		
Yang and Cao's protocol [19]			0/0/0		0/0/0		4/4/2		
Lai et al.'s protocol [11]			0/0/0		0/0/0		4/4/2		
Yoon-Jeon's protocol [20]			2/0/2		1/1/2		0/0/0		
Xie et al.'s protocol [18]			5/5/4		2/2/4		0/0/0		
Lee et al.'s protocol [12]			1/7	0/0	0/0	0/0	0/0		
	R         3         4         4         5         6         5         5         6         5         6         5         5         5         5         5         5         5         5         5         5         5         5         5         5         5         5         5         5         5	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	

Table 4: Cost comparison existing protocols for 3PAKE based on Chebyshev chaotic maps and our protocol

R Round, *RN* Random number, *PKE* Public key encryption, *SKE* Secret key encryption. *A*: participant A, *B*: participant B, *S*: Single Server, *SA*: ServerA, *SB*: ServerB, T, D, H and F represent the time for performing a Chebyshev polynomial computation, a symmetric encryption/decryption, a one-way hash function and pseudo-random function, respectively.

## 6 Conclusion

In this paper, we conduct a comprehensive and general study of two-party in different realms PAKE protocol over standard model using chaotic maps. Most existing researches are concerning about concrete environment, such as two-party AKE or three-party AKE based on chaotic maps, but as far as we know, there is no general and extensible architecture about different realms based on chaotic maps has been proposed. However, through our exploration, we firstly clarify that the PAKE scheme using chaotic maps in different realms is more suitable for the real environment. Then, we proposed a suitable protocol that covers those goals and offered an efficient protocol that formally meets the proposed security definition. Finally, after comparing with related literatures respectively, we found our proposed scheme has satisfactory security, efficiency and functionality. Therefore, our protocol is more suitable for practical applications. For the future, we will investigate some extended function, such as the group authenticated key agreement or resistant quantum attack authenticated key agreement in different realm.

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