# A Simple Password Authentication Scheme Based on Geometric Hashing Function

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# Abstract

Password authentication protocol is one of most important mechanisms to prevent resources from accessing by unauthorized users. Many password authentication schemes have been developed in last decades, and many of them are based on the use of smart card. However, nowadays it is not applicable for many applications on the Internet to adopt the smart card in their authentication scheme due to its inconvenience and relative high cost for both users and service providers. On the other hand, all password authentication schemes without using smart card (ex. a massive of smart card based password authentication schemes based on hash function) cited in this paper are proved to be vulnerable to replay attack and/or man-in-themiddle attack and/or verifier stolen attack, etc. Hence, in this paper, we focus on designing a simple, secure and high efficiency password authentication scheme based on geometric hash function without using smart card. Our security analysis and performance evaluation demonstrate that our scheme is quite simple and efficient, and also can withstand replay attack, password guessing attack, min-inthe-middle attack, verifier stolen attack and denial-ofservice attack.

Keywords: Geometric hash function, hash table, one-way hash function, password authentication

## **1** Introduction

In many insecure transmission environments, such as Internet and wireless channel, when a user wants to access the valuable recourse in the server, typically, a user's identity *id* and password *pw* are needed for the server to authenticate the validity of the user. Password authentication is one of the best-known and simplest

mechanisms for dealing with the transmission of secret data of a login system over insecure networks [21].

Traditional password authentication schemes store a verifier table for user authentication [8, 11, 12, 15, 16, 18]. In these schemes, generally, the user uses his/her identity id and password pw to login the system. In most cases, the identity id is considered as public, while the password pw is a secret. Many applications over Internet adopt this technique due to its easy to implement and relative low cost.

Recent decades, as the development of the smart cards, schemes have been proposed [2, 3, 14, 17, 19, 20, 22]. Many of these schemes are verifier free, which means that the server doesn't keep a verifier table for user authentication. However, each user in these systems needs to hold a smart card. Actually, these smart cards must be kept very carefully, because an attacker may compromise theses cards and steal all secrets in them, which could lead lots of security concerns. Besides that, compared with the traditional solutions, these schemes may increase the cost of both the users and the service providers due to the extra smart card.

In the real environment, it is not impossible for many applications to adopt smart cards due to its poor flexibility, especially for applications over Internet in which the service provider need to take into account the additional implementation cost [1]. Thus, in this paper, we focus on the group of schemes based on the use of verifier table without using smart card.

A straightforward method to ensure the data transmitted via an insecure channel is to adopt conventional encryption algorithm (such as RSA, DES and etc.). However, the heavy computation load on both the end-user and the server makes it is not suitable for real-time data exchange. Thus, many researchers began to focus on designing more lightweight password authentication schemes.

In 1981, Lamport [11] proposed a password authentication scheme based on one-way hash function to guarantee the secrecy of the password table in the server [7]. After that, an increasing amount of researchers proposed schemes [2, 3, 5, 9, 12, 15, 16, 18] to withstand various attacks, including off-line password guessing attacks, replay attacks, denial of service attacks, stolen-verifier attacks, and so on [21]. In 2000, Peyavian and Zunic [16] proposed a remote user authentication scheme based on hash function; however, since an intruder can easily get the user's identity id and two random numbers transmitted over an insecure channel, the intruder can obtain the user's password by off-line guessing. To overcome this drawback, Lee et al. [12] developed an improved scheme based on the work by Peyavian and Zunic [16]; however, as reported in [9], their scheme is also vulnerable to off-line guessing attack, denial-of-service attack and stolen-verifier attack. Sandirigama and Shimizu [18] proposed a efficient password authentication scheme named SAS (Simple And Secure password authentication). Unfortunately, Lin et al. [15] presented a replay attack and a DoS attack against SAS. They also proposed an improvement OSPA (Optimal Strong-Password Authentication) to repair the thoughtless designs of SAS. However, OSPA is also vulnerable to replay attack, stolen-verifier attack, DoS attack and guessing attack [4, 10, 13]. Later, Ku [8] developed a hash based password authentication scheme, which is proved to be vulnerable to the min-in-the-middle attack by Yang and Shen [23].

In this paper, we propose a very efficient password authentication scheme based on a geometric hashing without using smart card. Our scheme has the ability to withstand replay attack, password guessing attack, min-inthe-middle attack, verifier-stolen attack and denial-ofservice attack. Our scheme has another merit that the user's identity id never occurs in the insecure channel as a plain text, which can enhance the security of the protocol and protect the user's anonymity. The rest of the paper is organized as follows: Section 2 introduces the geometric hash function on which our scheme is based. In Section 3, our scheme is proposed. Section 4 provides security analysis and performance evaluation. The conclusions are drawn in Section 5.

# 2 Related Work

Comer and O'Donnell [6] proposed an efficient algorithm to produce a perfect hashing function of a set of keys in two-dimensional space. In this section, we will first give definitions related to the geometric problem and then describe their main idea about it. More details would not be discussed in this paper, because all concepts introduced in this section are enough for clarifying our scheme in later sections.



Figure 1: Example for introducing the definitions

Definitions and notations:

S: a set of *n* points in two-dimensional space,  $S = \{(x_i, y_i) | x_i, y_i \in R, 1 \le i \le n\}$ .

 $\theta$ : called angle of projection,  $\theta \in [0, \pi)$ . In two dimensional space, each angle corresponds to countless lines. For convenience, we always choose the one across the original point in computations through this paper.

 $|s_i|_{\theta}$ : The projection of point  $s_i$  at angle  $\theta$ . For  $s_i = (x, y)$ , the projection at angle  $\theta$  is

$$|s_i|_{\theta} = x \cdot \cos \theta + y \cdot \sin \theta \,. \tag{1}$$

 $P_{\theta}^{s}$ : A set of all projections of pairs in S at angle  $\theta$ ,

$$P_{\theta}^{s} = \{ \mid s_{i} \mid_{\theta} \mid \mid s_{i} \in S \}.$$

$$(2)$$

Usually, if S is known, we use notation  $P_{\theta}$  instead of  $P_{\theta}^{s}$ .

$$span(P_{\theta}) : \text{The span of } P_{\theta},$$
$$span(P_{\theta}) = \max(\left\| s_i \right\|_{\theta} - \left\| s_j \right\|_{\theta} \right\|, s_i, s_j \in S.$$
(3)

 $res(P_{a})$ : The resolution of projection  $P_{a}$ ,

$$res(P_{\theta}) = \min(\left\|s_i\right\|_{\theta} - \left|s_j\right\|_{\theta}), i \neq j \text{ and } s_i, s_j \in S.$$
(4)

 $len(P_{a})$ : The length of projection  $P_{a}$ ,

$$len(P_{\theta}) = \frac{span(P_{\theta})}{res(P_{\theta})}.$$
(5)

The geometric problem: find the angle of projection  $\theta \in [0, \pi)$  which minimizes  $len(P_{\theta})$  for a given *S*, a set of *n* points in two-dimensional space. For convenience, we always use the notation *GP* to represent this geometric problem in the rest of the paper.

Figure 1 gives an example to clarify aforementioned definitions. In Figure 1,  $S = \{s_1, s_2, s_3, s_4, s_5\}$ , and each point's  $(s_i)$  projection is denoted as  $p_i$ . Obviously, because the distance between  $p_1$  and  $p_5$  is longest,  $span(P_{\theta}) = ||s_1|_{\theta} - |s_5|_{\theta}|$ , and because the distance between  $p_2$  and  $p_3$  is shortest  $res(P_{\theta}) = ||s_2|_{\theta} - |s_3|_{\theta}|$ . Note that, the value of  $p_i$  is actually equals the distance between the original point and  $p_i$ . So, in Figure 1, the *GP* is to find an

angle of projection  $\theta$ , which leads a minimal value of  $len(P_{\theta}) = span(P_{\theta})/res(P_{\theta}) = (||s_1|_{\theta} - |s_5|_{\theta}|)/(||s_2|_{\theta} - |s_3|_{\theta}|).$ 

Index	Hashing value		
0	$P(\left (id_0, pw_0)\right _{\theta})$		$P((id_1, pw_2))$
1	null	-	$((\alpha_3, p, \gamma_3) _{\theta})$
2	$P(\left (id_1, pw_1)\right _{\theta})$		
<i>n</i> -1	null		
п	$P(\left (id_n, pw_n)\right _{\theta})$		

Figure 2: Example of the hash table

Obvously, we can change  $\theta$  from 0 to  $\pi$  to compute  $span(P_{\theta})$ ,  $res(P_{\theta})$  and then  $len(P_{\theta})$  for each  $\theta$ . Then, we find the expected  $\theta$  which produces the minimum  $len(P_{\theta})$  among all computed  $len(P_{\theta})$ 's. To reduce the time complexity, Comer and O'Donnell [6] offer an efficient way to solve the *GP*. Their algorithm presents a solution with time complexity  $O(n^2 \log n)$  [6]. For more details about their algorithm, please refer to the literature [6].

## **3** Proposed Scheme

In this section, we shall propose our scheme based on the *GP* introduced in Section 2. First, we give an overview of our scheme and then discuss the most important phases: registration phase, login phase and authentication phase as well as password changing phase.

In our password authentication scheme, the server holds a hash table which keeps a hash value for each record, as shown in Figure 2. If we consider each user's identity  $id_i$ and password  $pw_i$  as a point  $(id_i, pw_i)$  in two dimensional space, we can use the method introduced in [6] to compute the angle of projection  $\theta$  which minimize  $len(P_{\theta})$  for set  $S_{id}$ . pw, where  $S_{id-pw}$  consists of users'  $(id_i, pw_i)$  pairs. Obviously, that is exactly the *GP* problem. Using the method described in Section 2, we can compute the expected angle of projection and resolution for set  $S_{id-pw}$ .

Assume that we have computed the expected angle of projection  $\theta^*$  and the resolution *res* for  $S_{id-pw}$ . For a given pair  $s_i = (id_i, pw_i)$  in  $S_{id-pw}$ , we first compute its projection as follow:

$$P(|s_i|_{\theta}) = P(|(id_i, pw_i)|_{\theta}) = \cos\theta \cdot id_i + \sin\theta \cdot pw_i + C.$$
(6)

In Formula 6, the parameter *C* is a constant used to adjust the minimal projection of  $P_{\theta}^{S_{ideps}}$  to zero. This would be helpful to lead the hash table begin with index 0 in our later work.

$$C = -\min(\{P(\left|(id_j, pw_j)\right|_{\theta}) \mid P(\left|(id_j, pw_j)\right|_{\theta} \in P_{\theta}^{S_{id-pw}}\}). (7)$$

Next, we can compute the index of pair  $s_i = (id_i, pw_i)$  in the hash table by following formula:

$$Index(S_i) = Index(id_i, pw_i) = \left\lfloor P(|S_i|_{\theta}) / res(P_{\theta}^{S_{ul-pu}}) \right\rfloor.$$
(8)

After above work, given a pair  $s_i = (id_i, pw_i)$  in  $S_{id-pw}$ , we can adds its projection  $P(|s_i|)_{\theta}$  (hash value) into the hash table with index *Index*( $s_i$ ).

Three points worth noting here:

1) Because the resolution *res* is the minimal distance between any two different projections in  $P_{\theta}^{S_{ultpw}}$ , Formula (8) guarantee that there will never be any two different pairs which have the same index, which means that our hash function is perfect (no conflict). On the other hand, the size of the hash table equals  $\lfloor len(P_{\theta}^{S_{ultpw}}) \rfloor + 1$ . In Section 2, our task is to find a  $\theta$ which minimizes  $len(P_{\theta}^{s})$  for set *S*. Now, we can find

that the GP actually aims to find a minimal size and perfect hash table for a given set consisting of two dimensional elements.

- 2) Thanks to the constant *C* used to adjust the minimal projection of  $P_{\theta}^{S_{idpw}}$  to 0, the minimal index of the hash table is adjusted to 0.
- 3) Generally, each record just has one hash value. But for easy to maintenance the system, we attach a linked list to the record which is necessary to store more values. This case would happen in registration phase and password changing phase. More about this issue will be discussed in Subsection 3.1.

After creating the hash table, the server deletes the set  $S_{id-pw}$  and publishes the angle of projection  $\theta^*$ , resolution *res* and constant *C*. Note that, once the server has computed such a hash table, the set  $S_{id-pw}$  will be never used in future work. So, initially, our scheme needs to collect several (>= 2, theoretically) *id-pw* pairs for creating the hash table. For easy to describe all phases of our scheme, we assume that the server has computed such a hash table and published  $\theta^*$ , *res* and *C*.

#### 3.1 Registration Phase

The registration phase is invoked whenever a user wants to apply for a new account to join the system. The user first freely chooses his/her identity id and password pw, and then sends id and pw to the server via a secure channel. Upon receiving the registration request with pair (id, pw), the server does the following steps to respond it:

**R1**: The server uses Formula (6) to compute the projection  $P_{new}$  of pair (*id*, *pw*), and then uses Formula (8) to compute its index  $i_{new}$ .

**R2**: If  $i_{new}$  is bigger than or equal to the table size, the server extends the original table to size  $i_{new}+1$  ( $i_{new}$  is the last index), and adds  $P_{new}$  to the record with index  $i_{new}$ . Otherwise, server locates the record with index  $i_{new}$  and checks whether it is null. If it is null, server adds  $P_{new}$  to it directly; otherwise, two cases should be considered:

Case 1: If  $P_{new}$  is not equal to all projections in this record, the server attaches a list node with value  $P_{new}$  to this record.

Index	Hashing value	
0	$P(\left (id_0, pw_0)\right _{\theta})$	
1	$P(\left (id_{new1}, pw_{new1})\right _{\theta})$	
2	$P(\left (id_1, pw_1)\right _{\theta})$ -	$\mathbf{P}(\left (id_{new2}, pw_{new2})\right _{\theta})$
<i>n</i> -1	null	
n	$P(\left (id_n, pw_n)\right _{\theta})$	

Figure 3: Example of registration

Case 2: If  $P_{new}$  is equal to one of these projections in the record, the server rejects the registration request and prompts the user to choose a new identity *id*.

In our scheme, a very significant difference compared with other schemes is that, different users may have the same identity *id*, but never the same  $P(|id, pw|_{\theta})$ . Figure 3 is an example of registration. In Figure 3, there are two new users who choose their identities and passwords as  $(id_{new1}, pw_{new1})$  and  $(id_{new2}, pw_{new2})$ , respectively. The server then computes their projections and indexes by Formula (6) and (8). Assuming  $Index(id_{new1}, pw_{new1}) = 1$  and  $Index(id_{new2}, pw_{new2}) = 2$ , since the hashing value of index 1 is null, server adds  $P(|(id_{new1}, pw_{new1})|_{\theta})$  to it. Due to the value of

index 2 is not null and we assume that  $P(|(id_1, pw_1)|_{\theta}) \neq P(|(id_{new2}, pw_{new2})|_{\theta})$ , server attaches a link list to it.

#### 3.2 Login Phase

When a user wants to login the system, this phase will be first carried out.

**L1**: The user submits his/her identity  $id_r$  and password  $pw_r$  to a client.

**L2**: Upon reviving the request with pair  $(id_r, pw_r)$ , the client computes  $m_1 = P(|(id_r, pw_r)|_{\theta})$ ,  $m_2 = h(pw_r \oplus id_r)$ ,  $M_1 = Index(|(id_r, pw_r)|_{\theta})$ ,  $M_2 = h(m_1 \oplus t_c)$ ,  $M_3 = pw_r \oplus m_1$ ,  $M_4 = P(|(m_2, pw_r)|_{\theta})$ , where  $h(\cdot)$  denotes a one-way hash function and  $t_c$  is the time stamp. Then, the client sends the authentication messages  $M_1, M_2, M_3, M_4$  and  $t_c$  to server.

#### 3.3 Authentication Phase

The authentication phase is invoked when the server gets an authentication request.

**A1**: The server checks whether  $0 < t_s - t_c < t_r$ , where  $t_s$  is the current time stamp of the server and  $t_r$  is a reasonable time delay threshold. If it holds, next step is carried out; otherwise, the server rejects the request.

A2: If  $M_1$  is bigger than or equal to the table size, server rejects the request. Otherwise, the server uses the  $M_1$  as an index to locate the corresponding record in the hash table. If the value with index  $M_1$  is null, the server terminates current session; otherwise, the server uses each hash value  $P(|(id_i, pw_i)|_{\theta})$  in the record to compute  $M_2 = h(P(|(id_i, pw_i)|_{\theta}) \oplus t_c)$ . If one of these computed  $M_2$  is (assume by

using hash value  $P_m$ ) equals the received  $M_2$ , next step will be carried out; otherwise, the server terminates the current session.

**A3**: The server uses  $P_m$  to extract  $pw_e$  from  $M_3$  by  $M_3 \oplus P_m$ . Then the server uses  $pw_e$  and  $p_m$  can get the  $id_e$  utilizing Formula (6). After that, the server can compute a local  $m_2$ <sup>'</sup> =  $h(pw_e \oplus id_e)$  and  $M_4 = P(|(m_2, pw_e)|_{\theta})$ . If  $M_4$  equals the received one, the server approve the user's login request.

#### 3.4 Password Changing Phase

When a user wants to change his password, he first needs to login the system using his original identity  $id_o$  and password  $pw_o$ . If the user login the system successfully, then, following steps are performed.

**C1**: The user submits his new password  $pw_n$  to the client. The client then computes  $m = P(|(id_o, pw_n)|_{\theta})$  and transmits messages  $M_{C1} = m \oplus P(|(id_o, pw_o)|_{\theta})$  and  $M_{C2} = h(m) \oplus h(P(|(id_o, pw_o)|_{\theta}))$  to the server.

**C2**: Due to the pre-performed login and authentication phases, the server can note down the  $P(|(id_o, pw_o)|_{\theta})$  once the user successfully login the system. After receiving the message  $M_{C1}$ , the server can extract the *m*' by doing  $M_{C1} \oplus P(|(id_o, pw_o)|_{\theta})$ . And then the server computes  $h(P(|(id_o, pw_o)|_{\theta}))$  to extract h(m) from  $M_{C2}$ . Finally, the server uses the extracted *m*' to compute a local h(m') and check whether h(m) = h(m'). If it holds, next step will be carried out; otherwise, the server rejects the password changing request.

**C3**: The server uses Formula (8) to compute the new index of the user using the extracted  $P(|(id_o, pw_n)|_{\theta})$ . And handle this new index as the same way as the registration phase.

#### **4** Security Analysis and Performance Evaluation

Next, we will discuss the security of our scheme against various kinds of attacks and its performance efficiency. First of all, there is a very different point of our scheme compared with others. That is the user identity *id* is also can be considered as a secret of the user because it is never transmitted as plain text in our scheme. But the security of our scheme is not depended on this assumption.

#### 4.1 Security Analysis

In this subsection, we will discuss the ability of our proposed scheme to withstand replay attack, off-line guessing attack, stolen-verifier attack, denial-of-service attack and min-in-the middle attack.

## **Resistance to replay attack**

An attacker can intercept messages  $M_1$ ,  $M_2$ ,  $M_3$ ,  $M_4$  and  $t_c$  of a user's authentication messages in last session over an insecure channel. Because a time stamp is used in  $M_2$ , an attacker cannot replay all messages with the intercepted  $t_c$  directly. This attack can be detected by the server easily because  $t_s - t_c > t_r$ . So, the attacker may tries to changes  $t_c$ 

Table 1: Comparisons among our scheme and othersAssume each string used in these protocols has length L. In our scheme, the total number of strong one way hash function used depends on the current record used to authenticate the user., so that *n* represents the size of linked list attached to the current record

current record.									
	SAS [18]	OSPA [15]	Peyravian and Zunic's Scheme[16]	Lee-Li-Hwang's scheme[12]	Ku's scheme[8]	Our scheme			
Resistance to replay attack	no	no	no	no	no	yes			
Resistance to guessing attack	no	no	no	no	no	yes			
Resistance to verifier- stolen attack	no	no	no	no	no	yes			
Resistance to min-in- the-middle attack	no	no	no	no	no	yes			
Resistance to Dos attack	no	no	no	no	no	yes			
Storage space for each user in server	3L	3L	2 <i>L</i>	2 <i>L</i>	3 <i>L</i>	1 <i>L</i>			
Total messages transmitted in a single session	4	4	5	5	6	4			
Total rounds in a single session	3	3	3	3	3	1			
Total number of strong one way hash function used	8	11	3	3	12	4+ <i>n</i>			

to a closest time stamp  $t_{c'}$ . However, it is also useless This attack generally occurs in the verifier updating and reject the user's login request.

## **Resistance to off-line guessing attack**

As the same assumption made in Subsection 4.1, the attacker has stolen the authentication messages of a user,  $M_1, M_2, M_3, M_4$  and  $t_c$ . Although an attacker can utilize Formula (8) to compute the  $|P(|(id, pw)|_a)|$  by doing  $M_1 \times res$ , the attacker still cannot get the user's password because the attacker doesn't know the user's identity *id*. Even if the attacker get the user's *id* by some other ways, it is impossible for him to guess the password of the user because there are a lot of candidates pw' which satisfy the equation  $|P(|(id, pw)|_{o})| = |P(|(id, pw')|_{o})|$ .

## **Resistance to stolen-verifier attack**

The stolen-verifier attack means that if an attacker has stolen a verifier stored in the server, then s/he can use it directly to masquerade as an authorized user to login the system. In the proposed scheme, if an attacker has stolen a verifier stored in the hash table, he still cannot login the system. With the stolen verifier  $P_s$ , the attacker can forge messages  $M_1$  and  $M_2$ . However, due to the attacker doesn't know the user's password pw (the attacker also doesn't know the user's *id* just from the transmitted messages), he cannot forge messages  $M_3$  and  $M_4$ . Therefore, it is very difficult for the attacker to login the system without any information about the user's password.

## Resistance to denial-of-service (DoS) attack

because the server will compute a mismatched  $M_2$  using a password changing phase. The one-time password changed time stamp from the client, which leads the server authentication scheme needs a message from the user to invoke the verifier updating in the server side. However, because our scheme needn't to update user's verifier after each successful authentication, DoS attack is fully resisted in this situation. In the password changing phase, since a message  $M_{c2}$  used to ensure the data integrity, any modification of  $M_{c1}$  will be detected by the server. So, our scheme can withstand DoS attack.

## Resistance to man-in-the-middle attack

A man-in-the middle attack intercepts messages both from the server and user, and then sends opposite side the forged messages to deceive the server or user. The success rate of this attack is based on the data integrity protection mechanism used in protocol. In our scheme, messages  $M_3$ and  $M_4$  are used to keep the data integrity in the protocol, so that any modification of messages will be detected in the server side.

#### 4.2 Performance Evaluation

Under a perfect situation, our scheme can authenticate a user with time complexity O(1). However, due to the linked list attached to the hash table, the time complexity is increased to O(n), where n is the size of the longest linked list attached to the hash table. To maintenance the performance of the system, when the size of the longest linked list is larger than a given threshold, the server should to re-compute such a hash table. Fortunately, it is a quite easy task for the server because the server has stored all projections (the verifiers) of all users. The server can find out the new resolution using Formula (4) based on all projections in the hash table, and uses Formula (8) to [4] C. M. Chen and W. C. Ku, "Stolen-verifier attack on two new strong-password authentication protocols,"

As mentioned in Section 3, because the user's identity never occurs in the channel as plain text, the user's identity *id* also can be considered as a secret in our scheme. But the security of our scheme is not depended on this assumption. From the security analysis made above, even though a user publishes his/her identity *id*, an attacker also cannot get any clue about the user's password from the transmitted messages  $M_1$ ,  $M_2$ ,  $M_3$  and  $M_4$ . Thus, in our scheme, if a user can carefully keep his identity *id*, this could make the login phase become more secure. Due to the same reason, our scheme is user anonymous.

Table 1 is a comprehensive comparison of our scheme and others'. In Ku's scheme [8], because an attacker can guess a user's password by off-line manner, it is easy for the adversary to implement other attacks after getting the right password. From Table 1, it is obvious that our scheme is quite efficient in views of space cost and total rounds needed in a single session. The total number of strong one way hash function used in our scheme is 4+n, where *n* is the size of linked list attached to the current record. Fortunately, as we discusse above, it is quite convenience for the server to re-compute a new hash table which is conflict resistance, so, the *n* equals 0 in most cases.

## **5** Conclusions

In this paper, we have proposed a password authentication scheme based on a geometric hashing problem, without using smart card. The scheme emphasizes on the properties of simplicity, practicality and high efficiency. Due to the low computation cost in the login and authentication phase, our scheme can be used in the resource-limited environment where fast password authentication is needed. As the security analysis and performance evaluation shown in Section 4, our scheme is more efficient and secure than other schemes cited in Table 1.

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